

# TSTE85 FORMULAS

## Circuits

Transition activity  $\alpha = \alpha_{01} + \alpha_{10} = 2\alpha_{01} = 2\alpha_{10}$

Switch activity  $a = \sum_i \alpha_{01,i} C_i / \sum_i C_i$

Switched capacitance  $C_{sw} = a \sum_i C_i$

Dynamic power consumption  $P_d = f_{clk} C_{sw} V_{pp} V_{DD}$

Short-circuit power consumption  $P_{sc} = af_{clk} t_{sc} I_{peak} V_{DD}$

Propagation time  $t_p \propto V_{DD} / (V_{DD} - V_T)^r, 1 \leq r \leq 2$

## MOSFETs

Threshold voltage  $V_T = V_{T0} + \gamma \left( \sqrt{|V_{SB} - 2\Phi_F|} - \sqrt{|2\Phi_F|} \right)$

Weak inversion ( $V_{GT} < 0$ )  $I_D = I_{D0} (W/L) e^{-|V_{GT}|/(n_s V_\Theta)} (1 + \lambda V_{DS})$

where

$$V_\Theta \approx 26 \text{ mV} @ T = 300 \text{ K}$$

$n_s$  can be calculated from  $S = n_s V_\Theta \ln(10)$

Strong inversion ( $V_{GT} \geq 0$ )  $I_D = k' (W/L) V_{min} \left( |V_{GT}| - V_{min}/2 \right) (1 + \lambda V_{DS})$

where

$V_{min} = \min(|V_{GT}|, |V_{DS}|, |V_{DSAT}|)$  (corresponding to saturation, resistive, and velocity saturation modes)

Gate-oxide leakage  $I_G = k_1 W \left( V_{ox} / t_{ox} \right)^2 e^{-k_2 t_{ox} / V_{ox}}$

## Logic

Shannon's expansion theorem  $\overline{f(x, y, z, \dots, +, \cdot)} = f(\bar{x}, \bar{y}, \bar{z}, \dots, \cdot, +)$

Cofactors  $f_{\bar{x}} = f(x, y, z, \dots) \Big|_{x=0}, f_x = f(x, y, z, \dots) \Big|_{x=1}$

Expansion in sum and product  $f(x, y, z, \dots) = \bar{x} \cdot f_{\bar{x}} + x \cdot f_x = (x + f_{\bar{x}})(\bar{x} + f_x)$

Observability Don't Care set  $ODC_x = f_{\bar{x}} f_x + \bar{f}_{\bar{x}} \bar{f}_x$