## TSTE19

## Power Electronics

## Examination (TEN1)

| Time: | Wednesday $13^{\text {th }}$ J anuary 2016 at 8:00-12:00 |
| :--- | :--- |
| Place: | U4/U6 |
| Responsible teacher: Tomas J onsson |  |
|  | Will visit the exam location at 8:45 and 10. |
| Number of tasks: | 6 |
| Number of pages: | 8 |
| Allowed aids: | Calculator |
| Total points: | 70 |
| Notes: | A pass on the exam requires approx. 30 points. |
|  | Describe your calculations clearly and detailed, explaining <br> your methods, assumptions and equations used. |

## Question 1



Figure 1
a) A three phase diode rectifier acoording to Figure 1 has inductance, $L_{s}$, on the ac-side-and $L_{d}$ on the dc-side. Which inductance shall be large in order to obtain continuous current through the dc-load.
b) List the three most important parameters that defines the commutation of current between two diodes in a rectifier as of Figure 1. Give a short motivation why.
c) In a DC/ DC converter, inductance is commonly used for energy transfer between low and high-voltage sides. If the average voltage across the inductance is greater than zero during a time interval, what can you say about the shape of the inductor current during this interval?


Figure 2
d) What device parameters are required to determine the conduction losses of a MOSFET if the drain current is known?
e) List three types of semiconductors with turn-off capability.

## Question 2



Figure 3
A three phase thyristor rectifier as shown by Figure 3 is connected to a three phase voltage source with the phase-phase voltage Us=410 Vrms. The commutation inductance can be neglected.
a) Draw the waveform of the converter dc-side voltage $u_{v}$ (before the inductor $L_{d}$ ) for a firing angle $\alpha=30$ deg.
b) Draw the waveform of the source current, $i_{\text {sa }}$, in one phase.
c) Determine the displacement power factor.
d) Calculate the dc-load voltage, $\mathrm{U}_{\mathrm{d}}$, and dc-power considering a resistive load of 25 ohm .
e) Calculate the fundamental frequency source rms current ( $\mathrm{i}_{\text {sa }}$ ). Assume zero losses of the thyristor converter.

## Question 3



## Figure 4

In the buck converter in Figure 4, the current $i_{L}$ is continuous with an average of 5 A , and with a negligible ripple magnitude. The MOSFET T1 is operated with a switching frequency $\mathrm{f}_{\mathrm{sw}}=120 \mathrm{kHz}$ and a duty cycle in order to keep the capacitor voltage at 10 V for an input voltage $\mathrm{U}_{\mathrm{d}}=24 \mathrm{~V}$.
a) Determine the duty cycle of the MOSFET T1.
b) Calculate the conduction losses in the MOSFET T1 if the on-state resistance $\mathrm{R}_{\mathrm{ds}(\mathrm{on})}=0.05 \mathrm{ohm}$.
c) Calculate the turn-on losses in the MOSFET T1 if the rise time of the drain current is 40 ns . Current rises linearly and voltage is constant.
d) Calculate the turn-off losses in the MOSFET T1 if the fall time of the drain current is 60 ns . Current rises linearly and voltage is constant.
e) Determine the maximum allowed thermal resistance of the heatsink
( $\mathrm{R}_{\mathrm{th} \mathrm{AA}}$ ) for the MOSFET T1 in order to keep the heatsink temperature, $\mathrm{T}_{\mathrm{H}} \leq 60^{\circ} \mathrm{C}$ and the junction temperature, $\mathrm{T}_{\mathrm{J}} \leq 100^{\circ} \mathrm{C}$. The MOSFET has a thermal resistance $\mathrm{R}_{\text {thj }}=45.0^{\circ} \mathrm{C} / \mathrm{W}$. The ambient temperature, $\mathrm{T}_{\mathrm{A}}=25^{\circ} \mathrm{C}$. Note: $\mathrm{T}_{\mathrm{H}}$ or $\mathrm{T}_{\mathrm{J}}$ will equal the given limits, the other shall be lower.

## Question 4



Figure 5
A half-bridge voltage source converter is connected between a dc-source and an acload as shown by Figure 5. The control of the switched output voltage is done through pulse width modulation (PWM) with a switching frequency $\mathrm{f}_{\mathrm{sw}}=950 \mathrm{~Hz}$, in order to obtain a 50 Hz voltage component with a defined magnitude.
a) What is the minimum required dc-side voltage, $U_{d}$, required if the magnitude of the 50 Hz voltage component shall be 24 V rms when the amplitude modulation ratio, ma=0.9.
b) Calculate the current ripple in the output current, $\mathrm{I}_{\mathrm{v}}$, during the time interval shown in Figure 6. The time is defined based on the switching frequency cycle, $\mathrm{T}_{\mathrm{sw}}=1 / \mathrm{f}_{\text {sww }}$. During this time interval $\mathrm{U}_{\mathrm{ac}}=0.4^{*} \mathrm{U}_{\mathrm{d}}$, for the value of $U_{d}$ calculated in a). The inductance $L=3 \mathrm{mH}$. The initial current $\mathrm{I}_{\mathrm{v}}(\mathrm{t}=0)=0$.


Figure 6

## Question 5

The half-bridge converter in Figure 5 has a parasitic inductance, $\mathrm{L}_{\mathrm{c}}$, between the dc-source and the half-bridge. Figure 7 the switching waveform of the current through the MOSFET switch T1. The current $\mathrm{I}_{\mathrm{v}}=12$ A flows through L out of the converter.


Figure 7
a) Draw the waveform of the voltage across MOSFET T1, related to the current given in Figure 7 and considering the inductance $\mathrm{L}_{c}=40 \mathrm{nH}$. The dc-voltage $U_{d}=110 \mathrm{~V}$.
b) What is the peak voltage across the MOSFET?

## Question 6

A parallel capacitive snubber shall be designed for limitation of the peak voltage across the MOSFET switches of a half-bridge converter. The snubber, as shown by Figure 8, consists of a diode $D_{s}$, which will charge the snubber capacitor $C_{s}$ during over-voltage but prevent discharge when the MOSFET turns on. The dc-side voltage $\mathrm{U}_{\mathrm{d}}=110 \mathrm{~V}$. The design shall be based on the switching conditions related to a load current $\mathrm{I}_{\mathrm{v}}=12 \mathrm{~A}$.



Figure 8
a) Draw the waveforms of the current and voltage related to $\mathrm{T} 1, \mathrm{D} 2$ and Cs .

Assume the T1 current turn-off to be instantaneous as shown above. The snubber capacitor is initially charged to $\mathrm{U}_{\mathrm{c}}=\mathrm{U}_{\mathrm{d}}$ at the instant of T1 turn-off.
b) Calculate the required snubber capacitance in order to limit the over voltage to $20 \%$ when T 1 is turned off.

## Formula collection TSTE19 Power Electronics

## Fourier series coefficients using symmetry,

| Even | $f(-t)=f(t)$ | $b_{h}=0 \quad a_{h}=\frac{2}{\pi} \int_{0}^{\pi} f(t) \cos (h \omega t) d(\omega t)$ |
| :---: | :---: | :---: |
| Odd | $f(-t)=-f(t)$ | $a_{h}=0 \quad b_{h}=\frac{2}{\pi} \int_{0}^{\pi} f(t) \sin (h \omega t) d(\omega t)$ |
| Half-wave | $f(t)=-f\left(t+\frac{1}{2} T\right)$ | $a_{h}=b_{h}=0$ for even h |
|  |  | $a_{h}=\frac{2}{\pi} \int_{0}^{\pi} f(t) \cos (h \omega t) d(\omega t)$ for odd $h$ |
|  |  | $b_{h}=\frac{2}{\pi} \int_{0}^{\pi} f(t) \sin (h \omega t) d(\omega t)$ for odd $h$ |
| Even quart-wave | Even and half-wave | $b_{h}=0$ for all $h$ |
|  |  | $a_{h}=\frac{4}{\pi} \int_{0}^{\frac{\pi}{2}} f(t) \cos (h \omega t) d(\omega t)$ for odd $\mathrm{h}, a_{h}=0$ for even h |
| Odd quarter-wave | Odd and half-wave | $a_{h}=0$ for all $h$ |
|  |  | $b_{h}=\frac{4}{\pi} \int_{0}^{\frac{\pi}{2}} f(t) \sin (h \omega t) d(\omega t)$ for odd $\mathrm{h}, b_{h}=0$ for even h |

## Undamped resonant circuits

Even
Odd
Half-wave

$$
f(-t)=f(t)
$$

$$
f(-t)=-f(t)
$$

$a_{h}=0$
$a_{h}=b_{h}=0$ for even h
$a_{h}=\frac{2}{\pi} \int_{0}^{\pi} f(t) \cos (h \omega t) d(\omega t)$ for odd $h$
$b_{h}=\frac{2}{\pi} \int_{0}^{\pi} f(t) \sin (h \omega t) d(\omega t)$ for odd $h$
Even quart-wave Even and half-wave $b_{h}=0$ for all $h$
$a_{h}=\frac{4}{\pi} \int_{0}^{\frac{\pi}{2}} f(t) \cos (h \omega t) d(\omega t)$ for odd $\mathrm{h}, a_{h}=0$ for even h
Odd quarter-wave Odd and half-wave $a_{h}=0$ for all $h$
$b_{h}=\frac{4}{\pi} \int_{0}^{\frac{\pi}{2}} f(t) \sin (h \omega t) d(\omega t)$ for odd $\mathrm{h}, b_{h}=0$ for even h

## Integration rules

$$
\begin{aligned}
& \int_{a}^{b} f(x) d x=\int_{A}^{B} f(g(t)) g^{\prime}(t) d t \text { if } a=g(A), b=g(B) \text { and } g \text { is monotone in }[\mathrm{A}, \mathrm{~B}] \\
& \int_{a}^{b} \sin (x) d x=[-\cos (x)]_{a}^{b} \\
& \int_{a}^{b} \cos (x) d x=[\sin (x)]_{a}^{b}
\end{aligned}
$$

