# TSTE19 Power Electronics 

- Lecture 8
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## Outline

- DC-AC switching inverters 2
-Full-bridge inverter

-Harmonics

-DC-side current

## Half-bridge (2-level) converter

- DC-side midpoint '0' reference point for ac-output
- Output voltage switched between $+\frac{V_{d}}{2}$ and $-\frac{V_{d}}{2}$




## Full-bridge inverter

- M aximum output voltage doubled compared to halfbridge inverter
- No need for midpoint voltage



## PWM switching strategies

- Bipolar voltage switching
- Both pairs (TA+, TB-) and (TA-, TB+) controlled simultaneous
- 2 possible switch configurations

1. TA+, TB-: vA-vB positive
2. $T A-, T B+: v A-v B$ negative



## PWM bipolar switching

- Both legs switch at the same time

$$
\begin{aligned}
& \mathrm{m}_{\mathrm{a}}<1.0 \\
& \quad \hat{V}_{o 1}=m_{a} V_{d} \\
& \mathrm{~m}_{\mathrm{a}}>1.0 \\
& \quad V_{d}<\hat{V}_{o 1}<\frac{4}{\pi} V_{d}
\end{aligned}
$$



Figure 8-12 PWM with bipolar voltage switching.

## PWM modulation harmonics

- Harmonics as sidebands around multiples of switching frequency



## Harmonics due to $m_{a}$ and $m_{f}>9$

- For $\mathrm{m}_{\mathrm{f}}<9$ is harmonics almost independent of $\mathrm{m}_{\mathrm{f}}$
- Choose $m_{f}$ odd integer
- Odd symmetry
- Half-wave symmetry
- Only odd harmonics
- Even harmonics $=0$
- With $v_{A}=\hat{V}_{A} \sin \omega t$
all harmonics $\sin h \omega t$

Table 8-1 Generalized Harmonics of $v_{A o}$ for a Large $m_{f}$.

| $\boldsymbol{m}$ |  | $m_{a}$ |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Fundamental

| $m_{f}$ | 1.242 | 1.15 | 1.006 | 0.818 | 0.601 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $m_{f} \pm 2$ | 0.016 | 0.061 | 0.131 | 0.220 | 0.318 |
| $m_{f} \pm 4$ |  |  |  |  | 0.018 |
| $2 m_{f} \pm 1$ | 0.190 | 0.326 | 0.370 | 0.314 | 0.181 |
| $2 m_{f} \pm 3$ |  | 0.024 | 0.071 | 0.139 | 0.212 |
| $2 m_{f} \pm 5$ |  |  |  | 0.013 | 0.033 |
| $3 m_{f}$ | 0.335 | 0.123 | 0.083 | 0.171 | 0.113 |
| $3 m_{f} \pm 2$ | 0.044 | 0.139 | 0.203 | 0.176 | 0.062 |
| $3 m_{f} \pm 4$ |  | 0.012 | 0.047 | 0.104 | 0.157 |
| $3 m_{f} \pm 6$ |  |  |  | 0.016 | 0.044 |
| $4 m_{f} \pm 1$ | 0.163 | 0.157 | 0.008 | 0.105 | 0.068 |
| $4 m_{f} \pm 3$ | 0.012 | 0.070 | 0.132 | 0.115 | 0.009 |
| $4 m_{f} \pm 5$ |  |  | 0.034 | 0.084 | 0.119 |
| $4 m_{f} \pm 7$ |  |  |  | 0.017 | 0.050 |

Note: $\left(\hat{V}_{A 0}\right)_{h} / \frac{1}{2} V_{d} \mathrm{I}=\left(\hat{V}_{A N}\right)_{h} / \frac{1}{2} V_{d} \mathrm{~J}$ is tabulated as a function of $m_{a}$.

## 

 $i_{o}(t)=\sqrt{(2)} I_{o} \sin \left(\omega_{1} t-\varphi\right)$$V_{d} i^{*}{ }_{d}(t)=v_{o}(t) i_{o}(t)$
$i^{*}{ }_{d}(t)=I_{d}-\sqrt{(2)} I_{d 2} \cos \left(2 \omega_{1} t-\varphi\right)$

$$
\begin{gathered}
\text { where } \\
I_{d}=\frac{V_{o} I_{o}}{V_{d}} \cos \varphi \\
I_{d 2}=\frac{1}{\sqrt{(2)}} \frac{V_{o} I_{o}}{V_{d}}
\end{gathered}
$$




## -Unipolar (3-level) voltage switching

-Switches in each inverter leg (A and B) are controlled independently of the other leg
-4 possible switch configuration

1. $T A+, T B+: v A-v B=0$
2. $T A+, T B-: v A-v B>0$
3. TA-, TB-: $v A-v B=0$

4. TA-, TB+: vA $-\mathrm{vB}<0$


## Unipolar PWM-control

- One leg controlled by $\mathrm{v}_{\text {control }}$
- Other leg controlled by $-v_{\text {control }}$
- Four states



## PWM unipolar switching harmonics

- Harmonics at twice the switching frequency
- $m_{f}$ even makes switching frequency harmonic cancel out


PWM unipolar switching dc current

- Less ripple compared to bipolar switching



## 8-1

- In a single-phase full-bridge PWM inverter, the input dc voltage varies in a range of $295-325 \mathrm{~V}$. Because of the low distortion required in the output vow, $\mathrm{m}_{\mathrm{a}}<1.0$.
a) What is the highest $V_{01}$ that can be obtained and stamped on its nameplate as its voltage rating?
b) Its nameplate volt-ampere rating is specified as 2000 VA , that is, $\mathrm{V}_{\mathrm{o} 1, \text { max }} \mathrm{I}_{\mathrm{o} 1, \text { max }}=2000 \mathrm{VA}$, where $\mathrm{i}_{\mathrm{o}}$ is assumed to be sinusoidal. Calculate the combined switch utilization ratio when the inverter is supplying its rated volt-amperes.
c) Compare with results for a half-bridge.


## DC/DC-converter control

- Pulse width modulation, PWM, to control switching

- Switching frequency $f_{s}$
(a)

(switching frequency $f_{s}=\frac{1}{T_{s}}$ )
(b)

Figure 7-3 Pulse-width modulator: (a) block diagram; (b) comparator signals.

## Exersice 8-100

- In a half-bridge converter with $\mathrm{U}_{\mathrm{d}}=2 \mathrm{~V}$ and $\mathrm{L}=2 \mathrm{mH}$ switching is done with $\mathrm{m}_{\mathrm{a}}=0.8$ and $\mathrm{m}_{\mathrm{f}}=5$

- Construct graphically the output voltage and current, $\mathrm{u}_{\mathrm{v}}$ and $\mathrm{i}_{\mathrm{v}}$
- $u_{L}=L \frac{d i_{L}}{d t}$

$$
\Delta i_{L}=\frac{u_{v}-u_{a c}}{L} \Delta t
$$

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