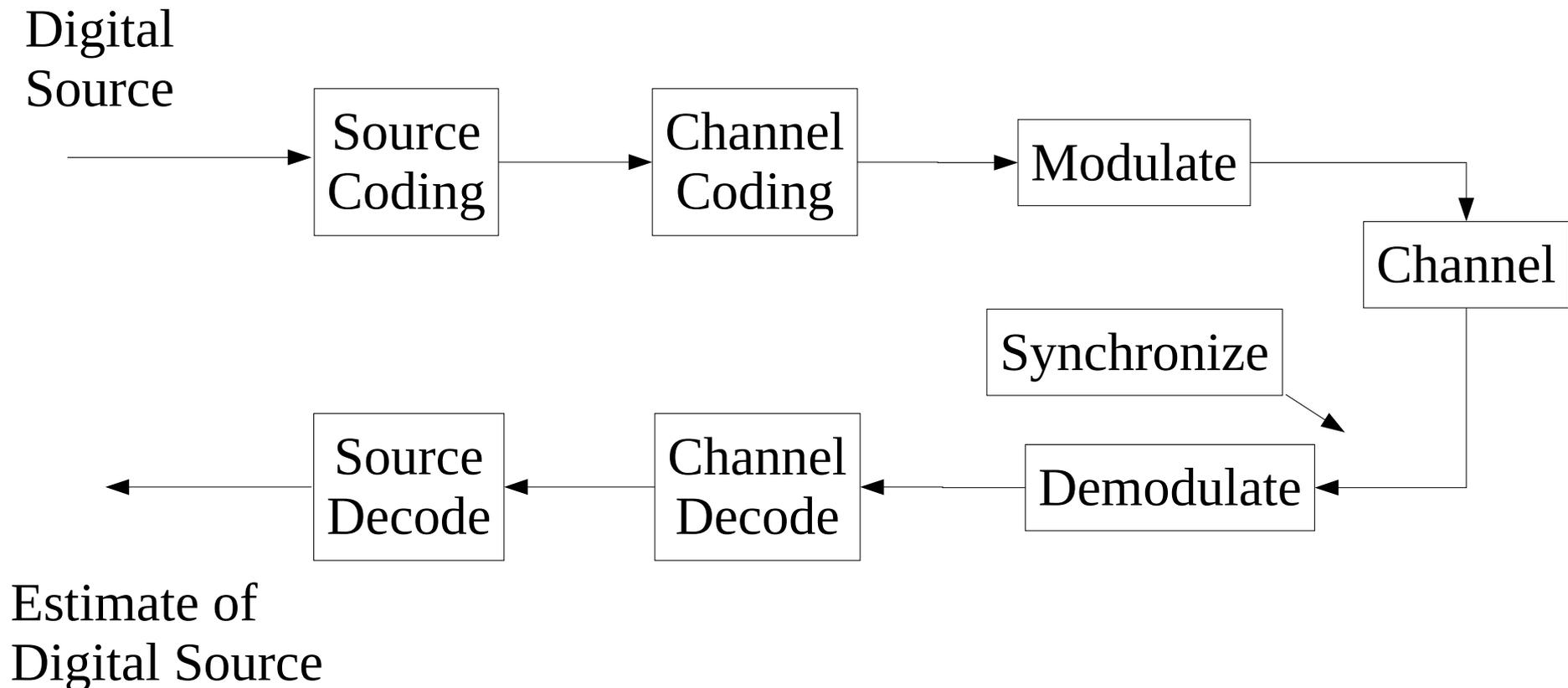


TSTE17 System Design, CDIO

- Introduction telecommunication
- OFDM principle
- How to combat ISI
- How to reduce out of band signaling

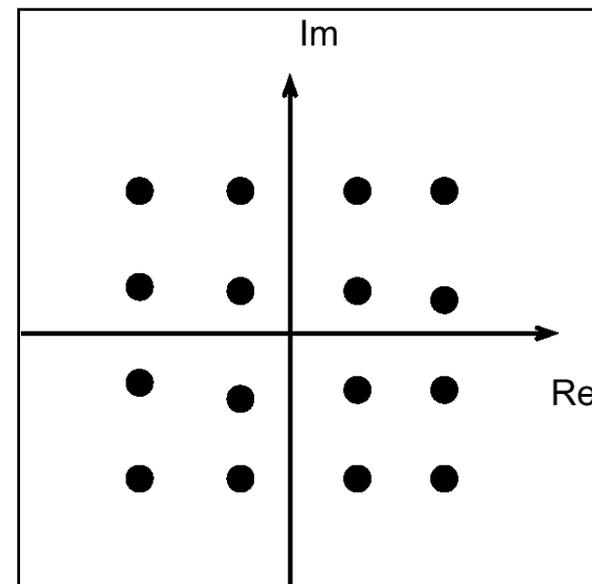
Components of a digital communication system



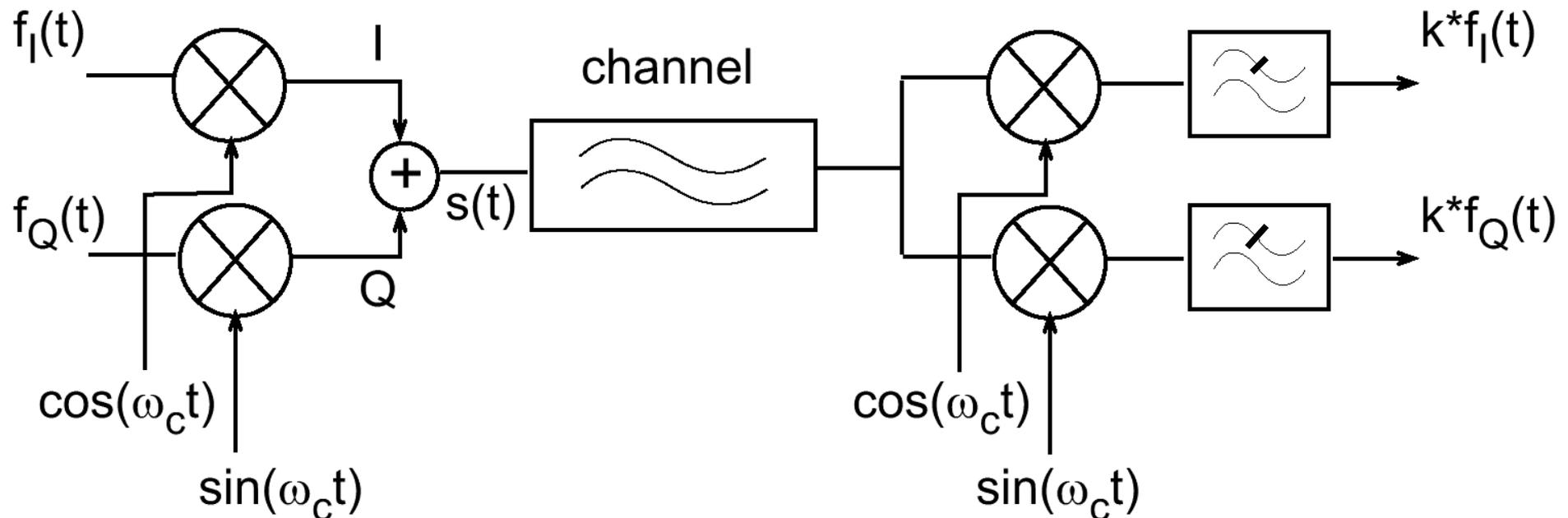
Quadrature Amplitude Modulation (QAM)

- Modulate both amplitude and phase
- Use equal distance between all points

16-QAM



Creating the modulated carrier



Wireless communication, cont.

- High data rate => Large bandwidth (BW)
- $BW \gg$ Coherence bandwidth => frequency selective fading
 - Coherence bandwidth = $1/T_m$ (multipath spread)
- Possible solutions
 - Use multiple narrow carriers
 - Use equalizer to even out effect (inverse of impulse response)

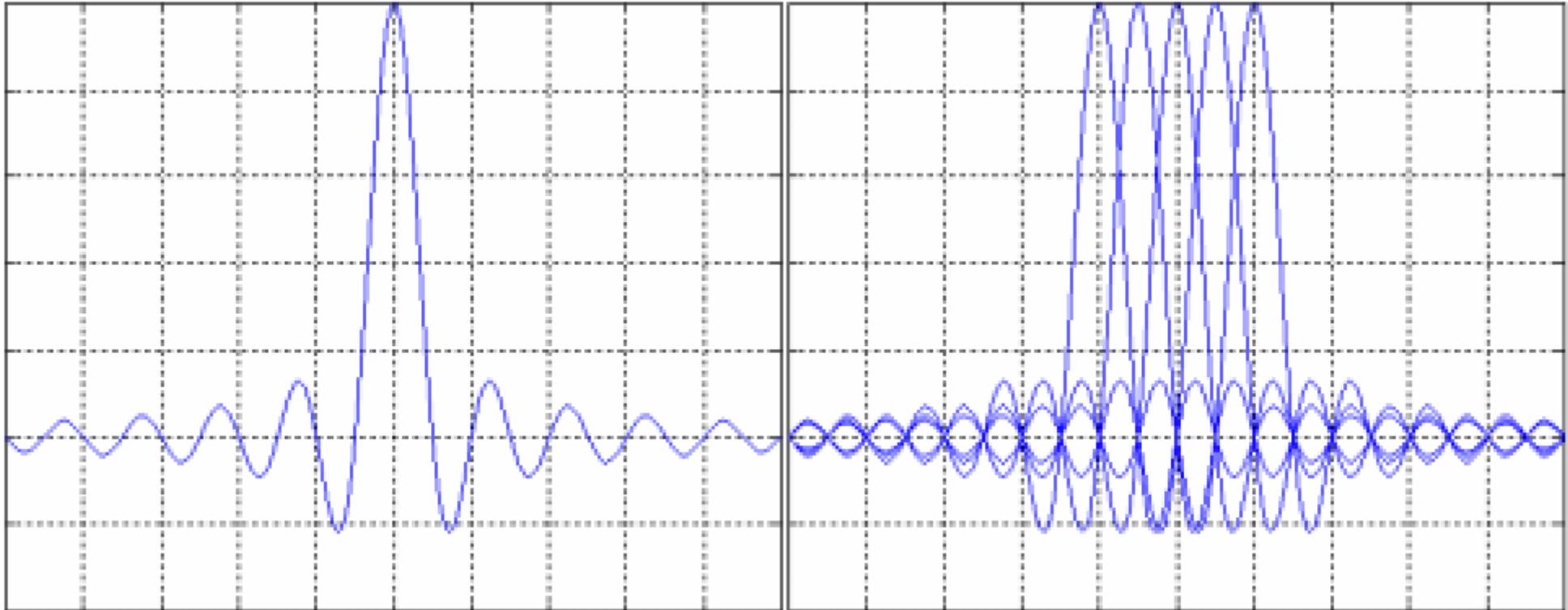
Multi-carrier Multiplexing

- Reduce effects of frequency selective fading by use of multiple carriers
- Each carrier must be non-overlapping with the other carriers to enable detection of data
- Leads to inefficient use of bandwidth

OFDM

- Use orthogonal carriers => better use of frequency spectrum
- Use integer number of periods for each carrier (carrier spacing $1/T_{\text{symbol}}$)
- Require that spectral peak of each carrier must coincide with the zero crossing of all other carriers

OFDM cont.



Single carrier frequency respons

Overlapping orthogonal carriers

Discrete Fourier Transform

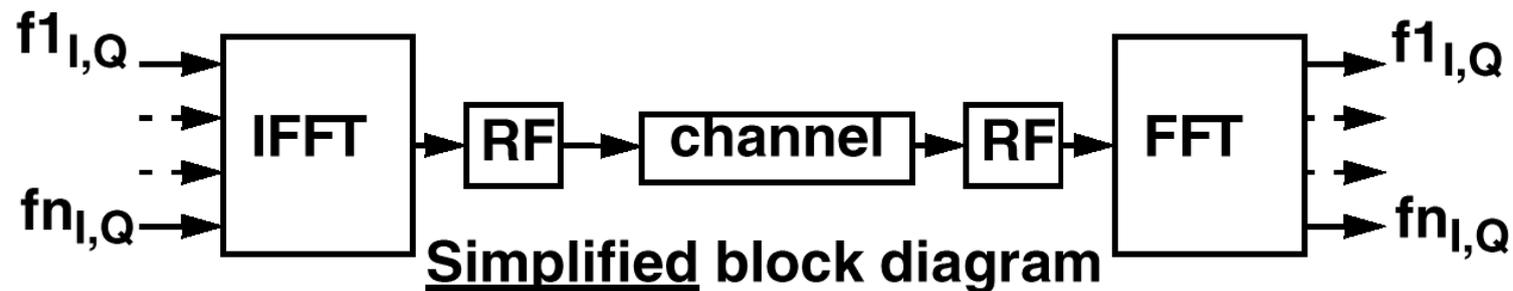
$$X(k) = \sum_{n=0}^{N-1} x(n) e^{-j2\pi kn/N}$$

$$x(n) = \frac{1}{N} \sum_{k=0}^{N-1} X(k) e^{j2\pi kn/N}$$

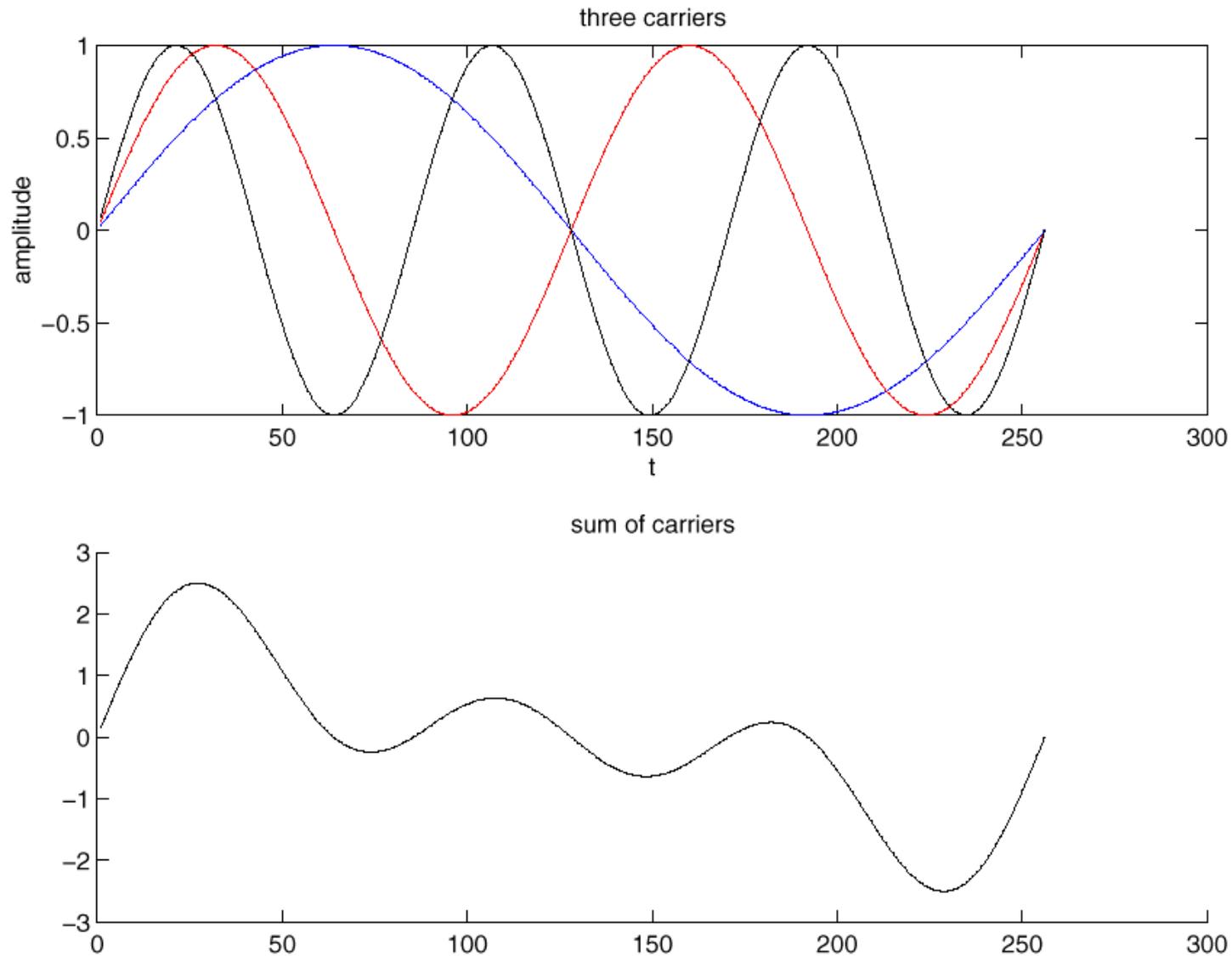
- Implemented using IFFT
 - $O(n \log n)$ complexity

OFDM cont.

- Let inputs to the IFFT be the constellation points
 - Each coefficient controls the phase and amplitude of the subcarrier
- Requires the IFFT and FFT to be synchronized



IFFT subcarriers, example

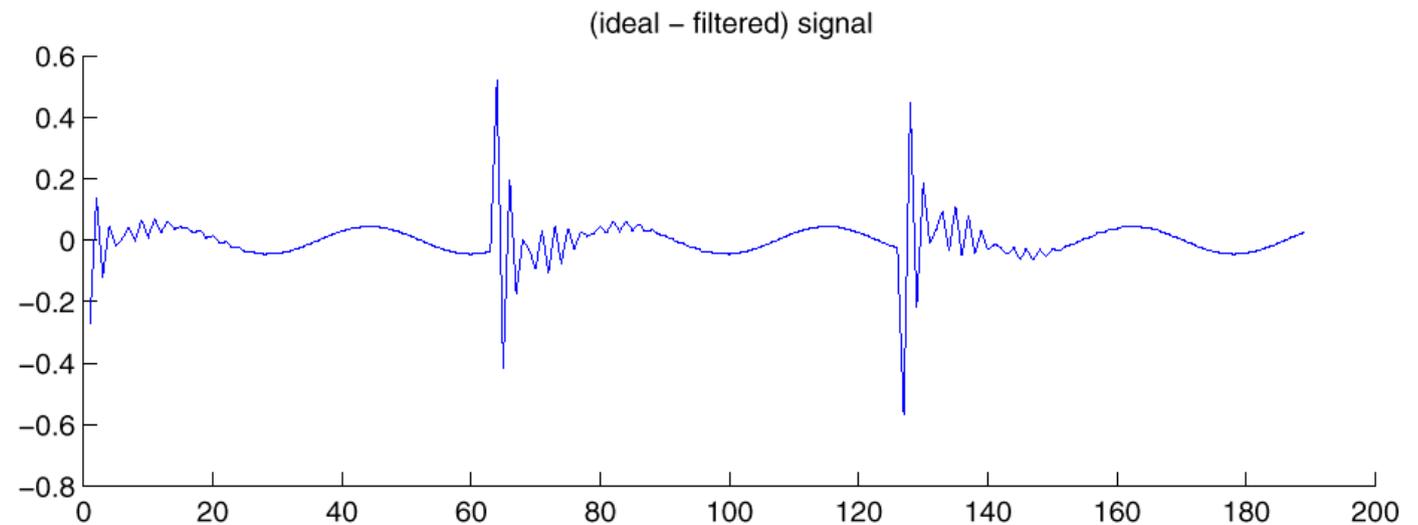
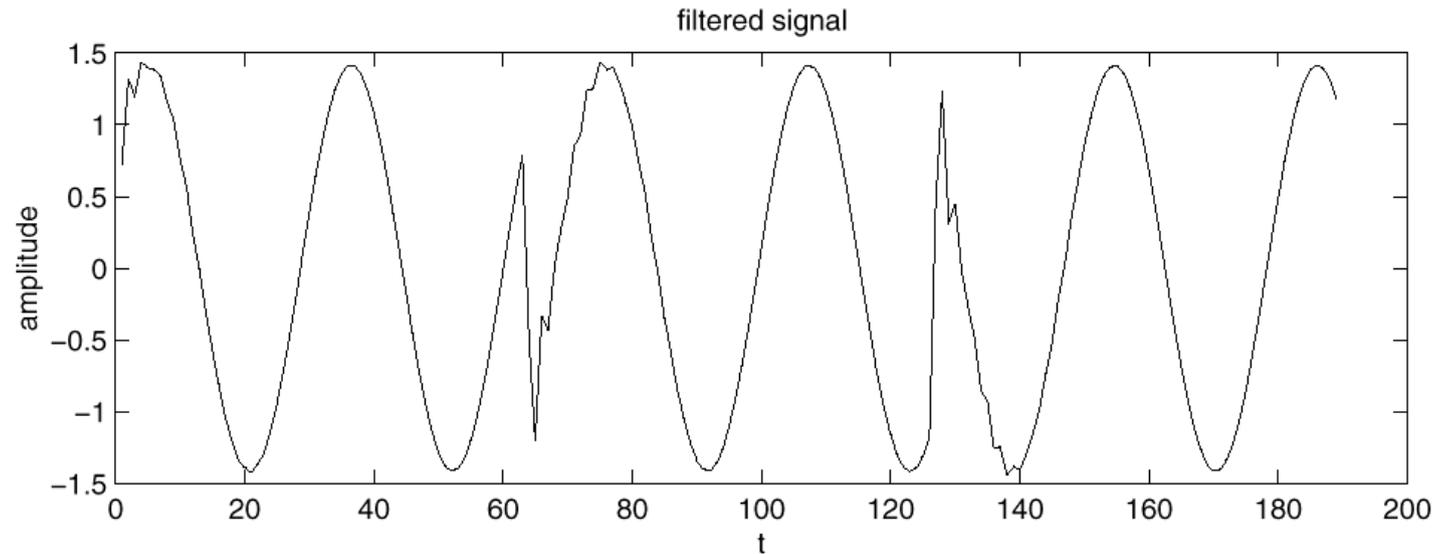


Avoiding Delay spread errors

- Inter Symbol Interference (ISI) caused by delay spread
 - Must avoid receiving multiple symbols
- Solution: Guard Intervals, do not send a new symbol until all delayed versions of the previous symbol has reached the receiver.
 - Empty transmission leads to Inter Carrier Interference (ICI)
- Guard interval $>$ channel impulse response length

Without Guard Interval

64
Point
IFFT

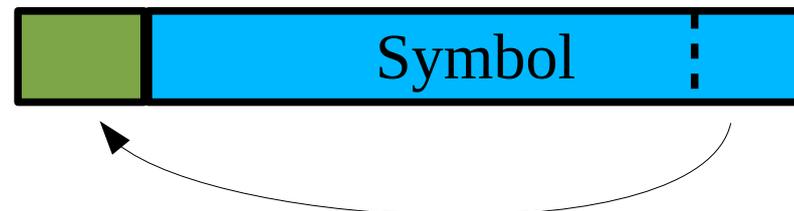


Without guard interval

- Adding scaled delayed versions of sinusoids
- Addition gives only a scaled and delayed signal
- Only works if the symbol length is increased without changing contents (frequency components)
- Remember the Discrete Fourier transform is cyclic!

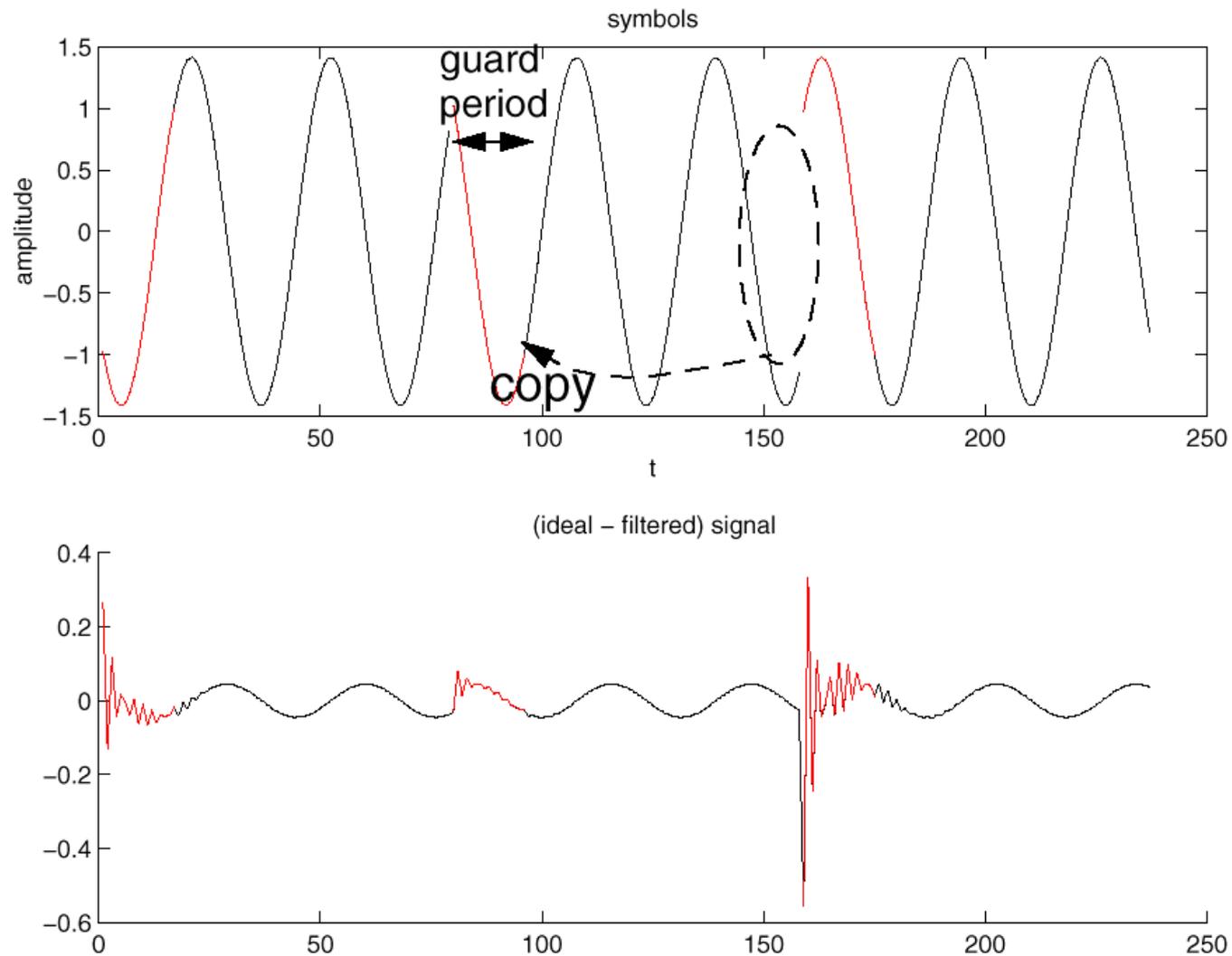
Guard Time

- Multipath => Mixing of two subsequent symbols in receiver
- Avoid mix by extending the symbol
 - Cyclic prefix



- Same information found independent where inside the symbol
 - Varies in phase only depending on start

With Guard Interval using Cyclic prefix



Cyclic prefix

- Two ways to increase symbol length
 - Prefix: Add copy of the end of the symbol to the front
 - Postfix: Add copy of the start of the symbol at the end
- Always gives a loss in data rate
 - Can be viewed as a reduction of power for each sent symbol
- Prefix can be changed to postfix by input rotation

Selection of parameters

- Dependency between cyclic pre/postfix length, delay spread, and number of subcarriers
 - Pre/post fix length $>$ delay spread
 - Pre/post fix length / Symbol length
 - Symbol Time = $1/\text{subcarrier distance}$
 - $N_{\text{carriers}} * \text{Subcarrier frequency} = \text{BW}$
 - $\text{Datarate on subcarrier} = \text{Total datarate} / N_{\text{carrier}}$

Parameter example

- $T_m = 300$ ns, Datarate = 50 Mbit/s, BW = 10 MHz, prefix/symbol length < 0.1
- Prefix at least 300 ns. Select guard interval = $4 * 300 = 1.2$ us (to be safe)
- Symbol time = $6 * \text{guard time} = 7.2$ us \Rightarrow guard time loss < 1 db
- Subcarrier distance = $1 / (\text{symbol time} - \text{guard interval}) = 1 / (7.2 - 1.2)$ us = 167 kHz
- Maximum number of subcarriers = BW / subcarrier distance = $10 / 0.167 = 60$

Parameter example, cont.

- 50 Mbit/s, 7.2 us symbol time =>
 $50 \cdot 10^6 * 7.2 \cdot 10^{-6} = 360$ bits/symbol
- $360/60 = 6$ bits / subcarrier. The modulation required would be 64-QAM
- Final design: 64 QAM modulation, 64 point IFFT (60 subcarriers used for data), $f_{\text{sample}} = 167 \cdot 10^3 * 64 = 10.67$ MSamples/s, 5 samples cyclic prefix, 69 samples long symbol.
- The above example could be modified to use lower datarate on a larger number of subcarrier

OFDM System

- Serial data stream to parallel data frames
- Modulate N subcarriers with BPSK, QPSK or QAM using the data frame
 - Data is in frequency domain (phase and amplitude for each subcarrier)
- Use IFFT for modulation (orthogonal subcarriers)
- Send the time domain signal

IFFT Algorithm

- Application of Divide and Conquer on the DFT transform
- Two approaches
 - Division in time
 - Division in frequency
- Complexity $O(n \log n)$

IFFT Algorithm

- Different ways to divide the input/output => different basic operation (butterfly)
 - Radix-2
 - Radix-4
 - Radix-8
- Tradeoff between number of operations and complexity of each operation

IFFT frequency map

- The input vector in frequency domain

[DC, f_c , $2f_c$, ..., $(N/2-1)f_c$, $(N/2)f_c$, $-(N/2-1)f_c$, ..., $-2f_c$, $-f_c$]

T : Symbol duration

$f_c = 1/T$: Subcarrier distance

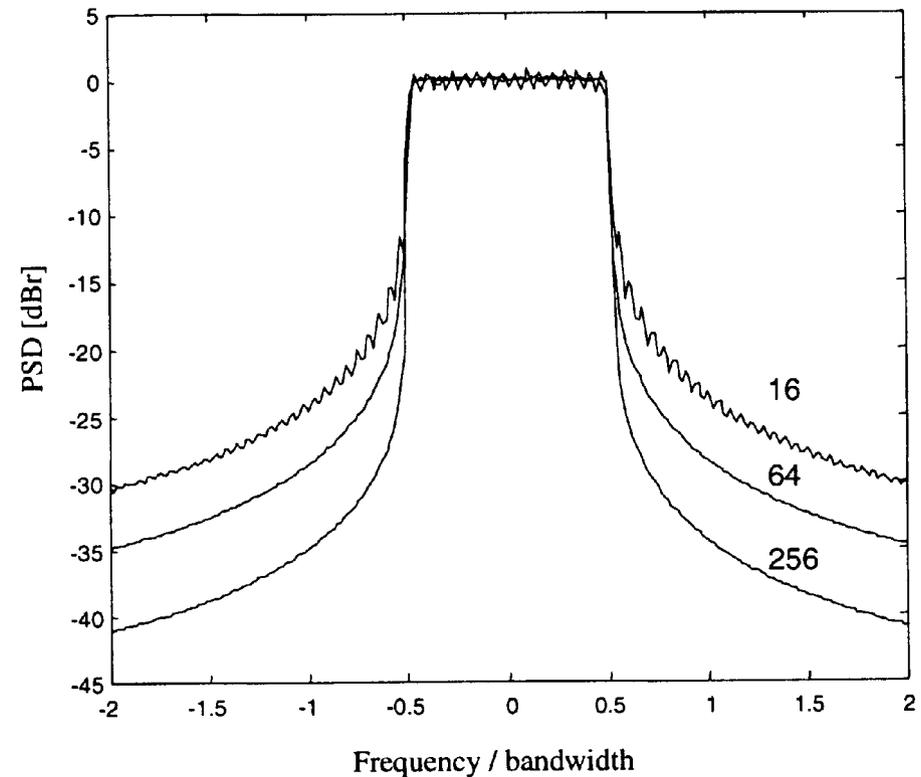
- DC and highest frequencies are usually not used
 - Requirements on A/D, D/A and mixers

Tricks with the IFFT

- Receiver FFT and IFFT can be designed simultaneously
 - Swap real and imaginary parts on input and swap real and imaginary parts on output
 - Rearrange order: 0, N-1, N-2, ... 2, 1
- Oversampling direct in the IFFT
 - Increase size of the IFFT, zero non-used channels
 - Increased computational load ($n \log n$ complexity)

Out of band spectrum

- IFFT generates unfiltered QAM subcarriers
- Transition between symbols generates out of band spectrum
- Reduced using windowing



Windowing

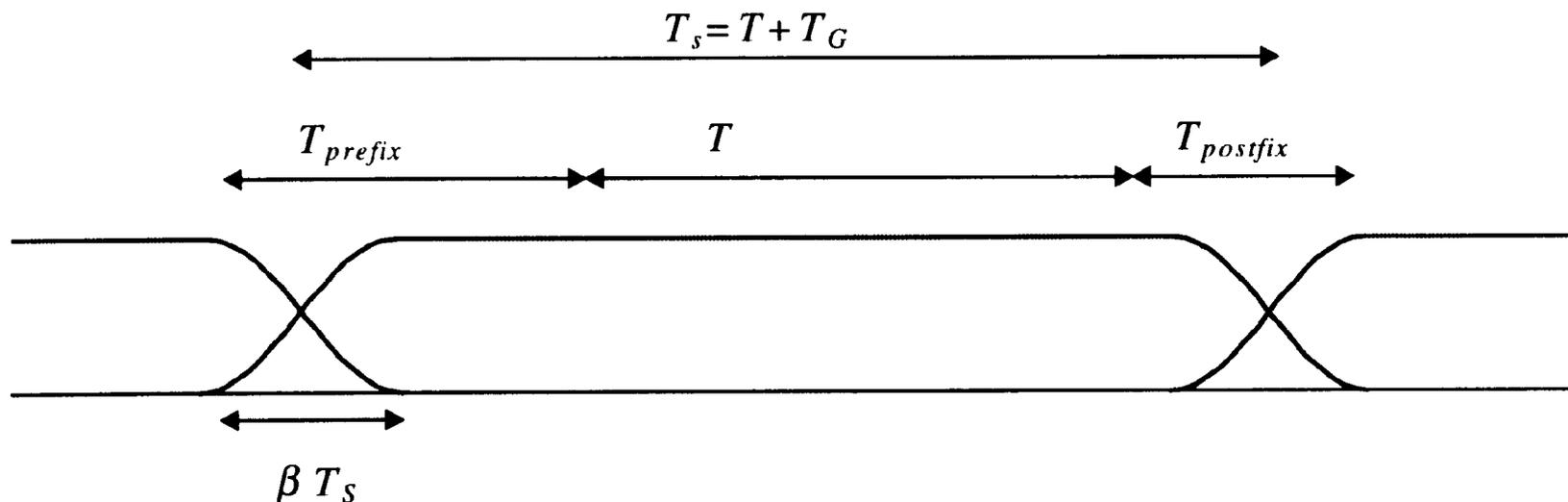
- Smooth the symbol transitions
- Common type
 - Raised cosine window

$$w(t) = \begin{cases} 0.5 + 0.5 \cos(\pi + t\pi / (\beta T_s)) & 0 \leq t \leq \beta T_s \\ 1, 0 & \beta T_s \leq t \leq T_s \\ 0.5 + 0.5 \cos((t - T_s)\pi / (\beta T_s)) & T_s \leq t \leq (1 + \beta)T_s \end{cases}$$

- T_s Symbol interval < Total symbol duration

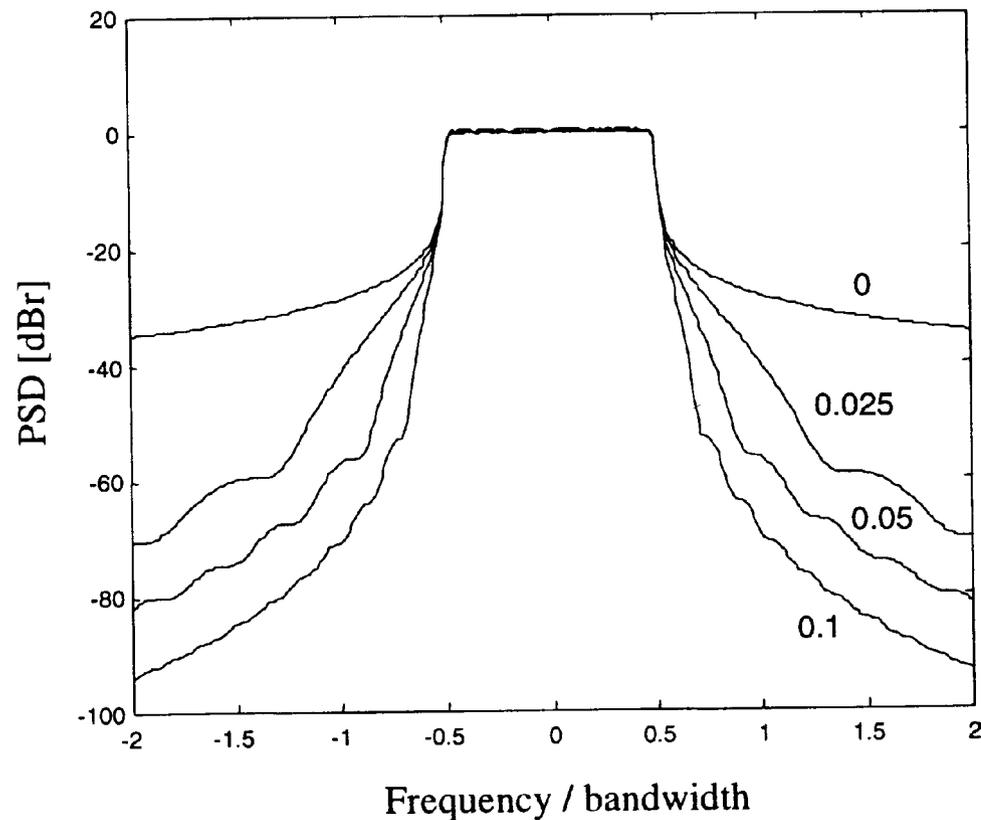
Windowing, cont.

- Windowing algorithm
 - T_{prefix} and/or T_{postfix} samples added
 - Multiply by raised cosine window $w(t)$
 - Add to output of previous symbol



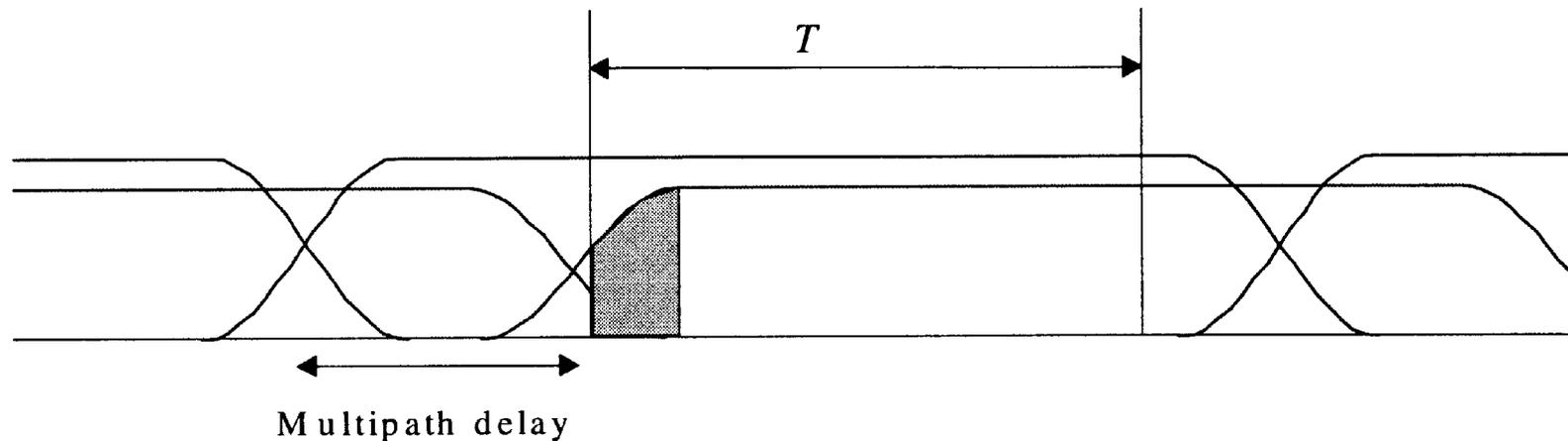
Windowing, cont.

- Small rolloff factor β gives large improvement



Windowing, cont.

- Large rolloff factor β reduces delay spread tolerance



Windowing, alternative

- Conventional filtering also possible
 - Convolution in time domain
- Must avoid ripple
 - Long ripple reduces delay spread tolerance
- Complexity higher
 - Windowing: a few multiplications per symbol
 - Filtering: a few multiplications per sample

OFDM Parameter Selection

- Input parameters
 - Bandwidth, bit rate, delay spread
- $T_{\text{guard}} \approx [2,4] * T_{\text{delayspread}}$
- $T_s \approx 5 * T_{\text{guard}}$
 - 1 dB SNR loss due to guard time
 - Longer symbol time => more subcarriers => more complex design & more sensitive to noise and frequency offsets

OFDM Parameter Selection, cont.

- Number of subcarriers
 - 3dB bandwidth / subcarrier spacing =
3dB bandwidth * $(T_s - T_{\text{guard}})$
- Alternative
 - Bit rate / bit rate per subcarrier
- Both alternatives depends on the modulation used
 - Comparison of modulation and channel coding

OFDM Parameter Selection, cont.

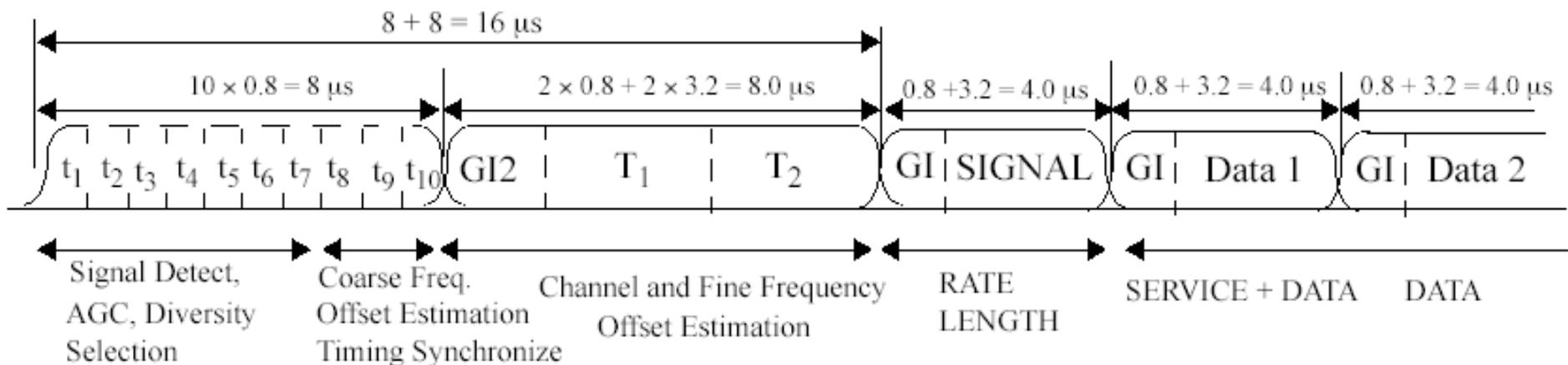
- Also important
 - Integer number of samples within the FFT/IFFT interval and symbol interval
 - Want the FFT/IFFT to be a power of 2
 - Need some of the subcarriers in the IFFT to be zero (oversampling)
 - May need to change some parameters slightly

Packet vs Continuous

- Continuous packet transmission
 - Digital Audio Broadcast (DAB)
 - Digital Video Broadcast (DVB)
 - No limit on synchronisation time
 - No multiaccess (sending data)
- Packet data transmission
 - Require fast synchronisation
 - Uses special training symbols (preamble)

802.11a Preamble

- Used to detect start of packet
- Used to synchronize receiver
- 10 short symbols + 2 long symbols



802.11a OFDM Parameters

- Bit rate 6, 9, 12, 18, 24, 36, 48, and 54 Mbps
- Modulation BPSK, QPSK, 16-QAM, 64-QAM
- Coding rates $1/2$, $2/3$, $3/4$
- Number of subcarriers 52 (4 pilots)
- OFDM symbol duration $4 \mu\text{s}$ (800 ns guard interval)
- Signal bandwidth 16.66 Mhz
- Subcarrier spacing 312.5 kHz

802.16 WirelessMAN-OFDM

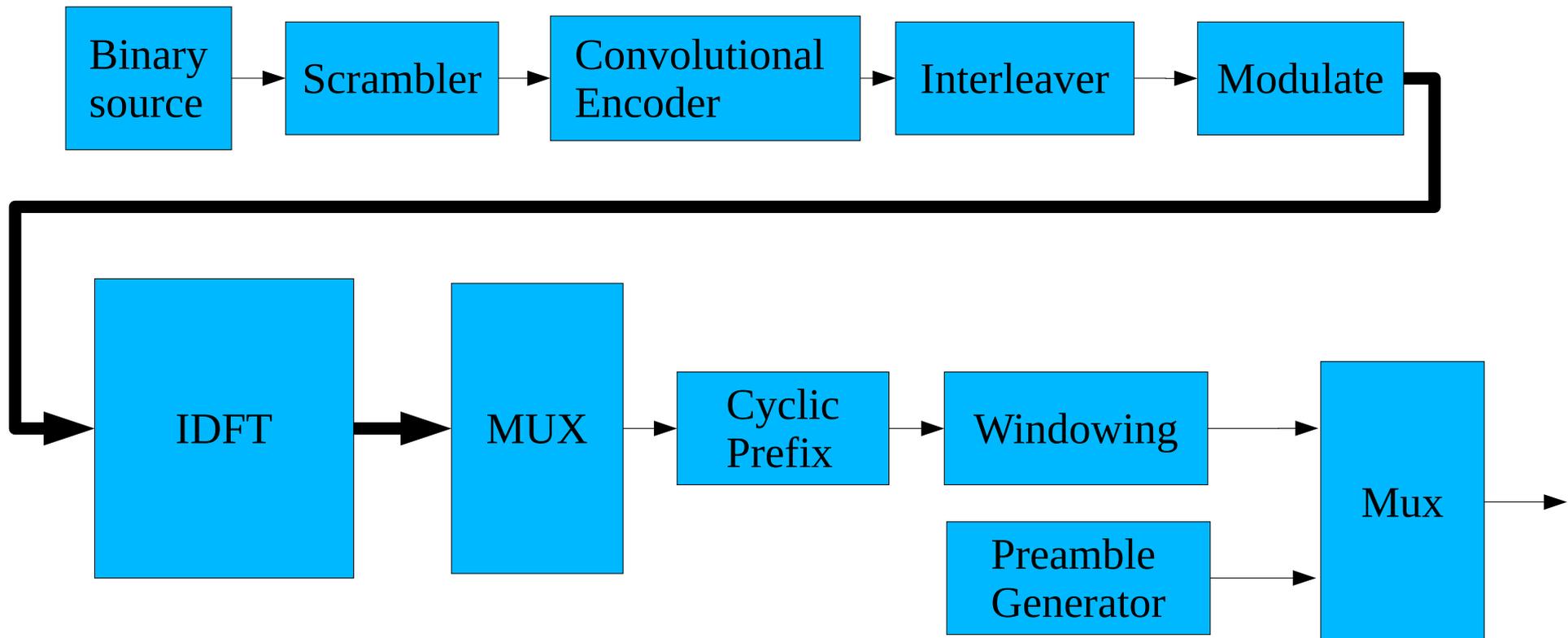
- One of 5 different Air interface standards
 - WirelessMAN-SC
 - WirelessMAN-SCa
 - WirelessMAN-OFDM
 - WirelessMAN-OFDMA
 - WirelessHUMAN

802.16 WirelessMAN-OFDM

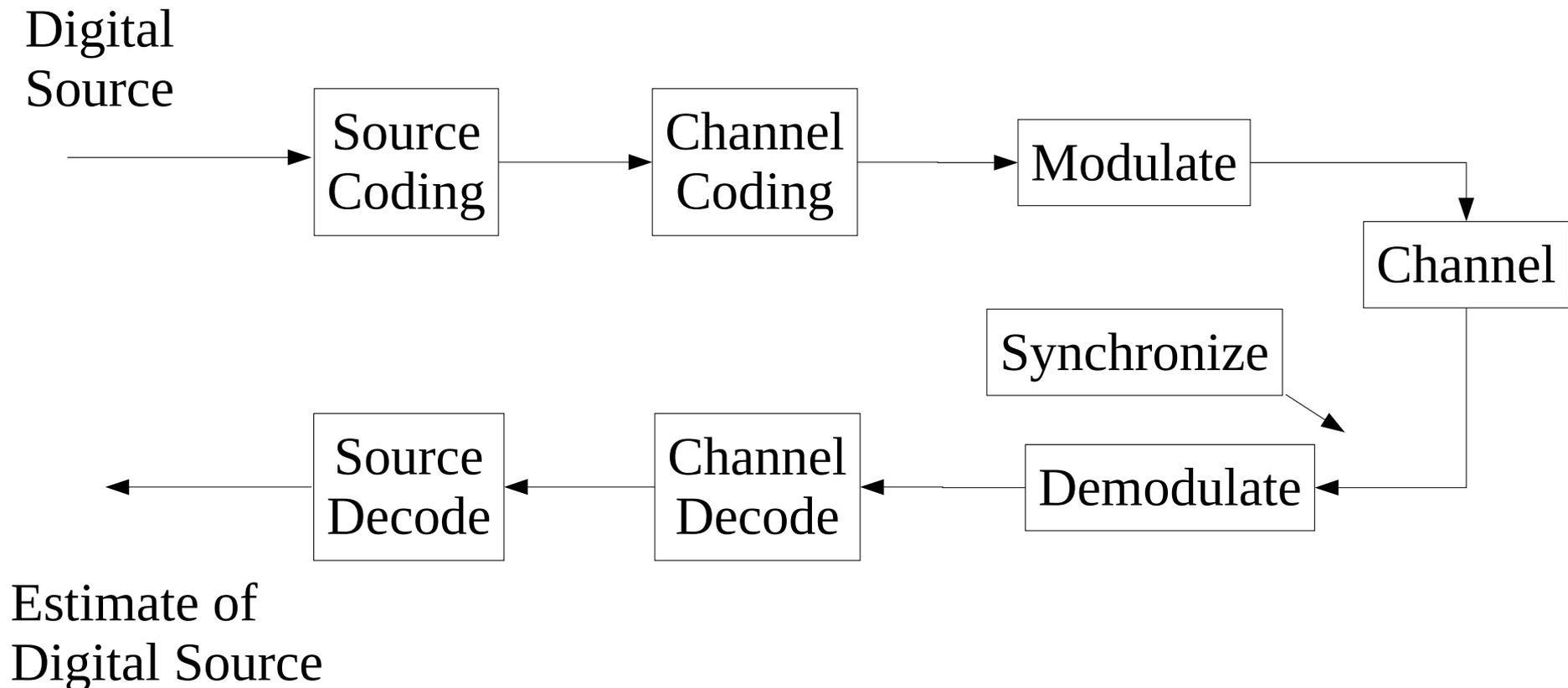
- Different options in standard
- 200 subcarriers used out of 256 available

802.11a & HiperLAN/2 Transmitter Details

- Excluding interpolation, A/D, and RF circuits

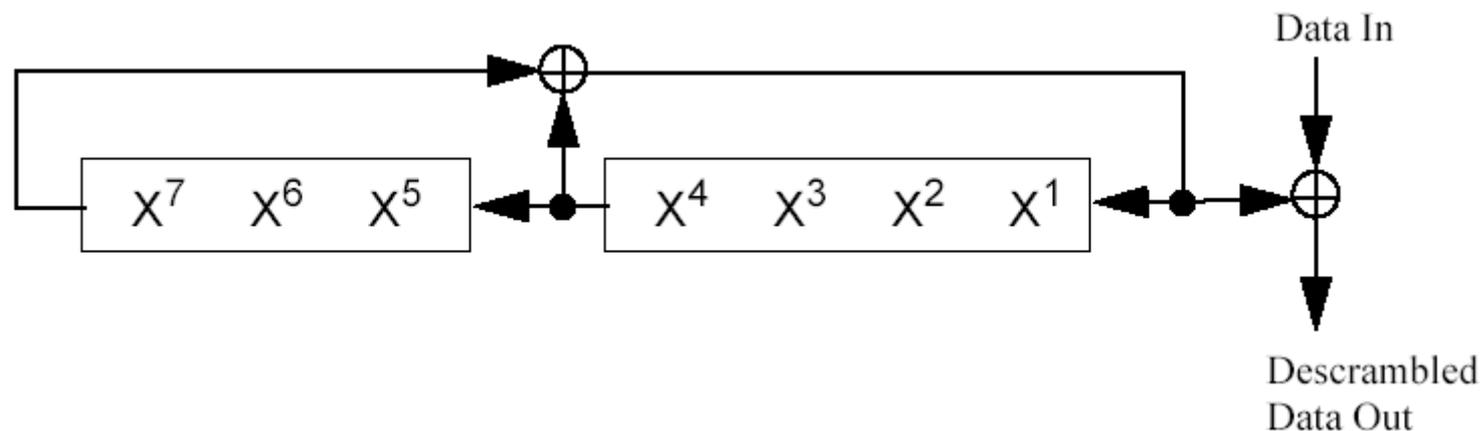


Components of a digital communication system



Scrambler

- Used to reduce probability of long sequences of 1 or 0.
- Pseudorandom sequences allows more efficient synchronisation at the receiver



802.11a vs HiperLAN/2 Physical Layer

HiperLAN/2

- Additional preamble
- Additional coding rate 9/16
- Possible to use 400 ns guard interval

802.11a

- Different initialization of the scrambler

Modulation details

- Three variables
 - Amplitude
 - Phase
 - Frequency
- Fixed subcarrier frequencies => Frequency modulation not possible
- Previously seen basic idea in BPSK, QAM etc.

Coherent and non-coherent modulation

- Coherent modulation
 - requires a phase lock between transmitter and receiver RF carrier waves.
 - Gives higher performance
 - Requires more complex receiver structure
- Non-coherent modulation
 - Simpler receiver structure
 - Can not use QAM, PSK, ASK