

$$\begin{aligned}
5.8 \text{ a) } \quad \| |F(e^{j\omega T})|^2 \|_p &= \sqrt[p]{\frac{1}{2\pi} \int_0^\pi | |F(e^{j\omega T})|^2 |^p d\omega T} = \\
&= \sqrt[p]{\frac{1}{2\pi} \int_0^\pi |F(e^{j\omega T})|^{2p} d\omega T} = \\
&= \left(\sqrt[p]{\frac{1}{2\pi} \int_0^\pi |F(e^{j\omega T})|^{2p} d\omega T} \right)^2 = \| |F(e^{j\omega T})|^2 \|_{2p}^2
\end{aligned}$$

b) We have:

$$\begin{aligned}
\| F(e^{j\omega T}) G(e^{j\omega T}) \|_p &= \sqrt[p]{\frac{1}{2\pi} \int_{-\pi}^\pi |F(e^{j\omega T}) G(e^{j\omega T})|^p d\omega T} \leq \\
&\leq \sqrt[p]{\frac{1}{2\pi} \int_{-\pi}^\pi |F(e^{j\omega T})|_{\max}^p |G(e^{j\omega T})|^p d\omega T} \leq \\
&\leq |F(e^{j\omega T})|_{\max} \sqrt[p]{\frac{1}{2\pi} \int_{-\pi}^\pi |G(e^{j\omega T})|^p d\omega T} \leq \\
&\leq \|F(e^{j\omega T})\|_\infty \|G(e^{j\omega T})\|_p, \quad p > 1 \\
\text{Hence, } \| F(e^{j\omega T}) G(e^{j\omega T}) \|_p &\leq \|F(e^{j\omega T})\|_\infty \|G(e^{j\omega T})\|_p, \quad p > 1
\end{aligned}$$