

4.4 The frequency response is

$$\begin{aligned}H(e^{j\omega T}) &= a + b e^{-j\omega T} + c e^{-j2\omega T} + b e^{-j3\omega T} + a e^{-j4\omega T} = \\&= e^{-j2\omega T} [a e^{j2\omega T} + b e^{j\omega T} + c + b e^{-j\omega T} + a e^{-j2\omega T}] = \\&= e^{-j2\omega T} [a \cos(2\omega T) + c + b \cos(\omega T)]\end{aligned}$$

$$\Phi(\omega T) = \arg\{ [\cos(2\omega T) - j \sin(2\omega T)] \} \pm n\pi = \arctan\left\{ \frac{-\sin(2\omega T)}{\cos(2\omega T)} \right\} \pm n\pi$$

$$\Phi(\omega T) = -2\omega T \pm n\pi \quad \text{Linear phase}$$

$$\tau_g(\omega T) = -\frac{\partial \Phi(\omega T)}{\partial \omega} = -2T \quad \text{Constant group delay}$$