

4.25 If the input values are repeated  $L$  times, the corresponding spectrum is

$$\begin{aligned}
 X(e^{j\omega T}) &= \sum_{m=-\infty}^{\infty} x_1(m) e^{-j\omega m T} = \sum_{n=-\infty}^{\infty} x(n) \sum_{k=0}^{L-1} e^{-j\omega k T} e^{-j\omega n T} = \\
 &= \sum_{n=-\infty}^{\infty} x(n) \frac{1 - e^{-j\omega L T}}{1 - e^{-j\omega T}} e^{-j\omega n T} = \\
 &= \sum_{n=-\infty}^{\infty} x(n) e^{-j\omega(L-1)T/2} \frac{\sin(\omega L T/2)}{\sin(\omega T/2)} e^{-j\omega n T}
 \end{aligned}$$

Hence, the spectrum is weighted with a  $\frac{\sin(Lx)}{\sin(x)}$  function that attenuates the unwanted images of the baseband, but it effects also the passband of interest. Compare this case with a zero-order-hold D/A converter. However, the attenuation is small and the computations must be done at the higher sample rate. Thus, the computational workload is much higher.