## **TSTE86 Homework 2: Solution**

Identify logic function from gate schematic

$$F(A, B, C, D, E) = \overline{\left(\overline{A+B}\right)} \cdot \overline{\left(\overline{C+D}\right) \cdot \overline{E}} = \overline{\left(A+B\right)\left(C+D+E\right)}$$

Switch nets

$$\begin{cases} S_{p} = F\left(\overline{A}, \overline{B}, \overline{C}, \overline{D}, \overline{E}\right) = \overline{\left(\overline{A} + \overline{B}\right)\left(\overline{C} + \overline{D} + \overline{E}\right)} = AB + CDE\\ S_{n} = \overline{F\left(A, B, C, D, E\right)} = (A + B)(C + D + E) \end{cases}$$

Transistor schematic with annotated widths,  $W_k$ 

$$A \xrightarrow{-} W_{1} \xrightarrow{C \xrightarrow{-} W_{3}} V_{DD}$$

$$A \xrightarrow{-} W_{1} \xrightarrow{D \xrightarrow{-} W_{3}} D \xrightarrow{-} W_{4}$$

$$B \xrightarrow{-} W_{2} \xrightarrow{E \xrightarrow{-} W_{5}} F(A, B, C, D, E)$$

$$A \xrightarrow{-} W_{6} \xrightarrow{B \xrightarrow{-} W_{7}} F(A, B, C, D, E)$$

$$A \xrightarrow{-} W_{8} \xrightarrow{D \xrightarrow{-} W_{9}} \xrightarrow{E \xrightarrow{-} W_{10}} W_{10}$$

Select all channel lengths to minimum,  $L_{\min}$ , and express the widths in units of  $L_{\min}$ . Worst case resistance occurs when a single path conducts. Design the widths of a single conduction path to be equal. Using  $R \propto 1/W$ , we should design the two pull-up paths to have an equivalent resistance of  $W_p = 5L_{\min}$ :

$$\begin{cases} \frac{1}{W_1} + \frac{1}{W_2} = \frac{1}{5} & \text{equal widths in path} \\ \frac{1}{W_3} + \frac{1}{W_4} + \frac{1}{W_5} = \frac{1}{5} & W_1 = W_2 = 10 \\ W_3 = W_4 = W_5 = 15 \end{cases}$$

Design the six pull-down paths to have an equivalent resistance of  $W_n = 3L_{min}$ :

$$\begin{cases} W_6^{-1} + W_8^{-1} = 3^{-1} \\ W_6^{-1} + W_9^{-1} = 3^{-1} \\ W_6^{-1} + W_{10}^{-1} = 3^{-1} \\ W_7^{-1} + W_8^{-1} = 3^{-1} \\ W_7^{-1} + W_9^{-1} = 3^{-1} \\ W_7^{-1} + W_9^{-1} = 3^{-1} \\ W_7^{-1} + W_{10}^{-1} = 3^{-1} \\ W_7^{-1} + W_{10}^{-1} = 3^{-1} \end{cases} \begin{cases} W_6 = W_8 = 6 \\ W_6 = W_{10} = 6 \\ W_7 = W_8 = 6 \\ W_8 = W_9 = 6 \\ W_9 = W_{10} = 6 \\ \end{array}$$

Hence  $W_1 = W_2 = 10 L_{\min}$ ,  $W_3 = W_4 = W_5 = 15 L_{\min}$ , and  $W_6 = W_7 = W_8 = W_9 = W_{10} = 6 L_{\min}$ .