

Written Test
Course code: TSTE08, Exam code: TENA
Analog and Discrete-time Integrated Circuits (ISY)

Date:	August 25, 2009
Time:	8-12
Place:	G32
Number of exercises:	5 (5 points max. for each exercise)
Grades:	10p for 3 (ECTS: C), 15p for 4 (ECTS: B), and 20p for 5 (ECTS:A).
Allowed material:	All types of calculators except laptops. All types of official tables and handbooks. Textbooks: Johns & Martin: Analog Integrated Circuit Design. Razavi: Design of Analog CMOS Integrated Circuits. Sedra&Smith: Microelectronic Circuits. Dictionaries.
Examiner and responsible teacher:	Sune Söderkvist
Course administrator:	Sune Söderkvist. Tel.: 281355, mail: sune@isy.liu.se
Visiting today:	Around 9.30 and 11.00 a.m.
Correct (?) solutions:	Solutions and results will be on the webb home page for the course.

**Graded exams are returned on examiner's office times, tuesdays and
fridays at 11.00-13.00, during week no. 37 and 38.**

Students instructions

- The CMOS transistor operation regions, small-signal parameters, and noise characteristics are found on the last page of this exam.
- Generally, do not just answer yes or no to a short question. You always have to answer with figures, formulas etc., otherwise no or fewer points will be given.
- You may write down your answers in Swedish or English.

Good Luck!

Exercise 1.

In this example we will study the small-signal properties of the capacitive-loaded amplifier in **Figure 1**. Assume that the transistors small-signal parameters are g_{m1} , g_{mbs1} , g_{ds1} and g_{m2} , g_{mbs2} , g_{ds2} respectively.

- a) Sketch a small-signal equivalent circuit and determine an exact expression for the transfer function $H(s) = V_{out}(s)/V_{in}(s)$. The bulk effect can **not** be neglected. However, all capacitors but C_L can be neglected. Also, determine the DC gain. (4p)
- b) Determine an exact expression for the small-signal output resistance, r_{out} . (1p)

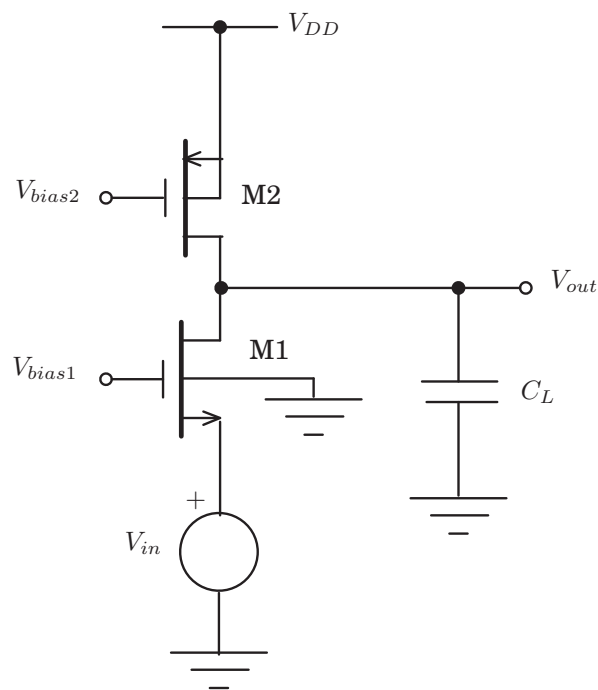


Figure 1: Gain stage.

Exercise 2.

Show that, for appropriate value of V_{bias} , equal voltage at the output and input can be obtained for the cascode stage in **Figure 2**. Assume that both transistors are operating in the saturated region. The channel-length modulation can be neglected. The transistors **M1** and **M2** have threshold voltages V_{tn} and V_{tp} respectively. The expression for V_{bias} may include V_{in} , V_{tn} and V_{tp} ; no other voltages.

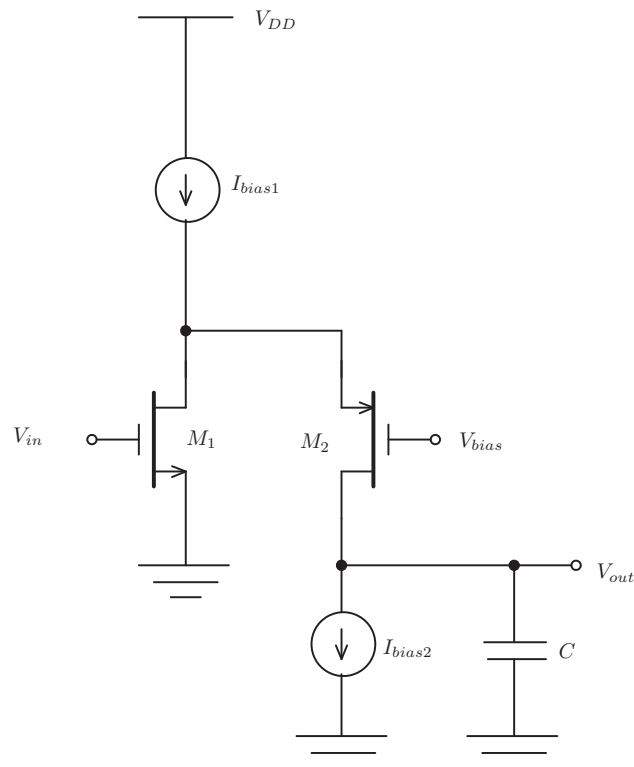


Figure 2: Folded cascode stage.

Exercise 3.

- a) Derive the common-mode range, CMR, and the output range, OR, of the circuit in **Figure 3**. You don't know anything about the relationship between sizes of different transistors. Threshold voltages may be different for all transistors. Anyhow all transistors are saturated.

The voltages should be expressed in currents I_{Di} , constants α_i , threshold voltages V_{tni} and V_{tpi} . (3p)

- b) What type of circuit is this?

The circuit can be seen as two different stages that are cascaded. What kind of stages are those two stages?

Why are transistors **M7** and **M8** included in the construction? (2p)

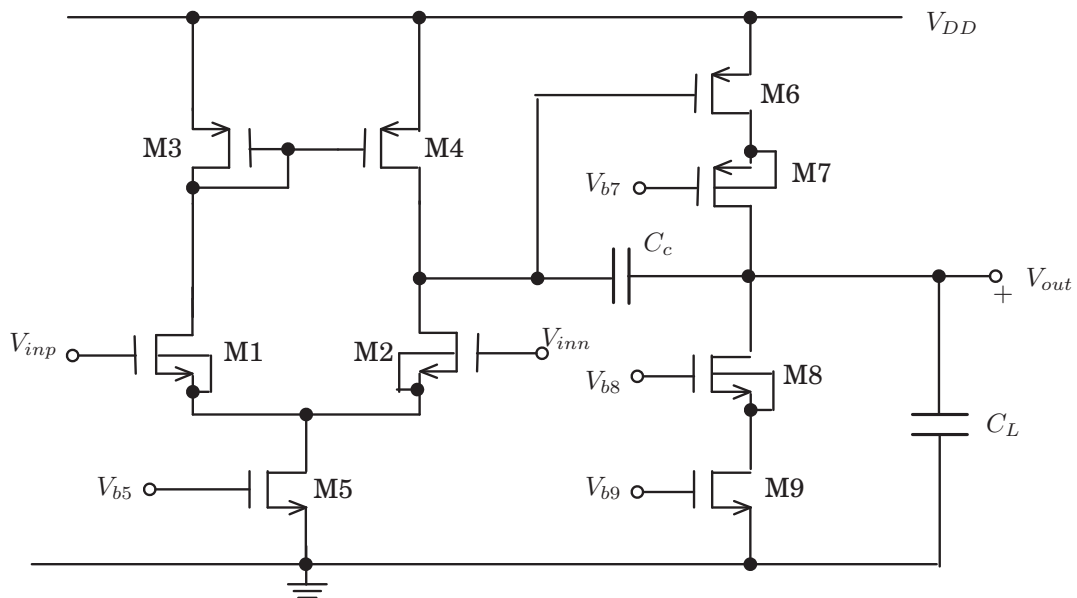


Figure 3: Transistor circuit.

Exercise 4.

Consider the two cascaded common-source stages in **Figure 4**, where only the thermal noise generated in the transistors is of interest. The current sources are ideal and hence noiseless. Let the output load capacitance be given by C_L and parasitic capacitances are only given by gate-source capacitance, C_{gs2} , for **M2**. Further $I_{bias1} = I_{bias2} = I_{bias}$. The transistors are identical with the small signal parameters $g_{m1} = g_{m2} = g_m$ and $g_{ds1} = g_{ds2} = g_{ds}$. Both transistors operate in the saturation region.

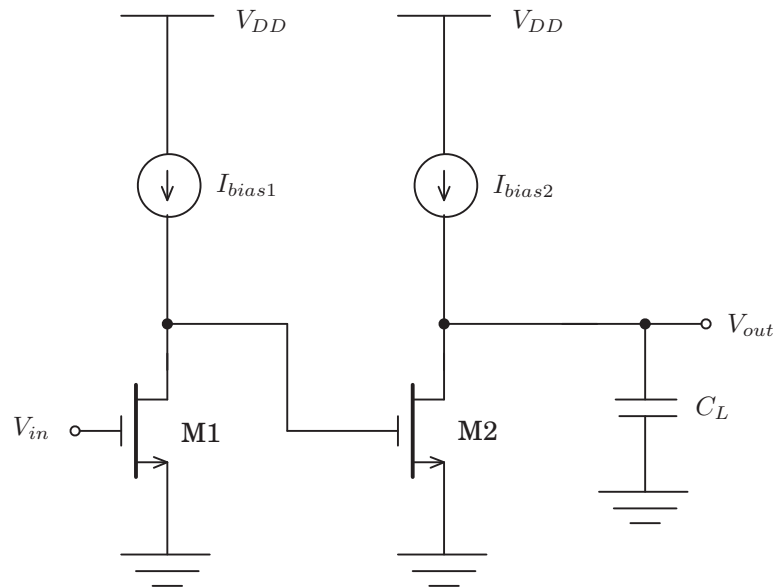


Figure 4: A noisy multi-stage amplifier.

Determine an expression for the spectral density R_{out} of the output thermal noise assuming that the noise from the transistors are uncorrelated.

Exercise 5.

Figure 5 shows an analog reference filter and a signal flow graph received after first synthesizing a leapfrog filter and then using a LDI-transformation followed by $z^{-1/2}$ propagation. In next step, intending to realize a SC-filter, the factors $z^{-1/2}$ in $\frac{R}{R_g}z^{-1/2}$ and $\frac{R}{R_L}z^{-1/2}$ are deleted, among other things. That is actually equivalent to replacing R_g and R_L with $R_g z^{-1/2}$ and $R_L z^{-1/2}$ respectively.

Now focus R_g and show that this operation means that R_g changes to a resistor R'_g parallel to a capacitor C_x .

To compensate for that new capacitor you can change the value of capacitor C_1 in the original analog reference filter. Determine the expression for this new capacitor C'_1 !

Also determine the constant s_0 so that a cut-off frequency $f_{ac} = 100$ kHz for the analog filter will give a cut-off frequency $f_c = 100$ kHz for the SC-filter. Sample period is $T = 1 \mu\text{s}$.

LDI-transform:

$$s = s_0(z^{1/2} - z^{-1/2})$$

$$\omega_a = 2s_0 \sin \frac{\omega T}{2}$$

Hint: Study $\frac{1}{\frac{z^{1/2}}{R_g}}$

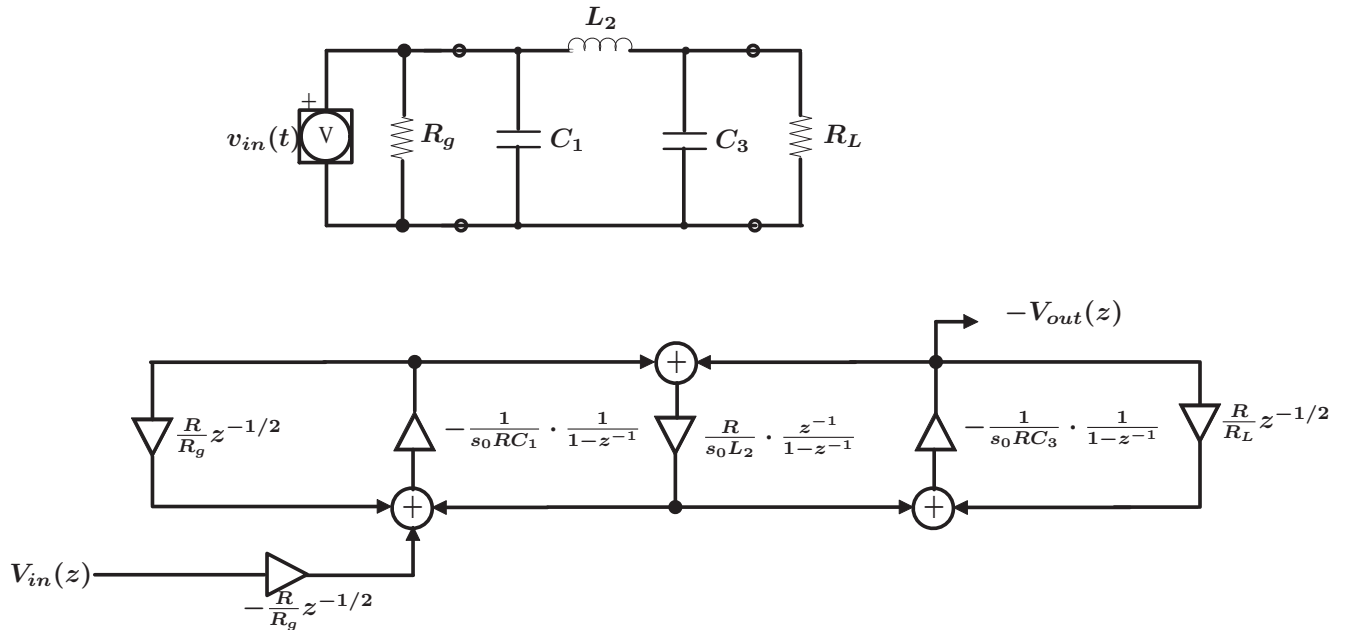


Figure 5: Analog filter and signal flow graph.

Transistor formulas and noise

1 CMOS transistors

Current and threshold voltage formulas and operating regions for an NMOS transistor

$$\begin{aligned}\text{Cut-off:} \quad & V_{GS} < V_t & I_D \approx 0 \\ \text{Linear:} \quad & V_{GS} - V_t > V_{DS} > 0 & I_D = \alpha(2(V_{GS} - V_t) - V_{DS})V_{DS} \\ \text{Saturation:} \quad & 0 < V_{GS} - V_t < V_{DS} & I_D = \alpha(V_{GS} - V_t)^2(1 + \lambda(V_{DS} - V_{eff})) \\ & & V_{DSsat} = V_{eff} = V_{GS} - V_t \\ \text{All regions:} \quad & V_t = V_{t,0} + \gamma(\sqrt{2\phi_F - V_{BS}} - \sqrt{2\phi_F})\end{aligned}$$

Small-signal parameters

$$\begin{aligned}\text{Linear:} \quad & g_m \approx 2\alpha V_{DS} \quad g_{ds} \approx 2\alpha(V_{GS} - V_t - V_{DS}) \\ \text{Saturation:} \quad & g_m \approx 2\sqrt{\alpha I_D} \quad g_{ds} \approx \lambda I_D\end{aligned}$$

$$\text{Constants:} \quad \alpha = \frac{1}{2}\mu_{0n}C_{ox}\frac{W}{L} \quad \lambda = \sqrt{\frac{K_s\epsilon_0}{2qN_A\phi_0}} \cdot \frac{1}{L} \quad \gamma = \frac{\sqrt{2qN_AK_s\epsilon_0}}{C_{ox}}$$

2 Circuit noise

Thermal noise in CMOS transistors

The thermal noise spectral density at the gate of a CMOS transistor is

$$V^2(f) = \frac{8kT}{3} \cdot \frac{1}{g_m}$$

Thermal noise in resistors

The thermal noise spectral density of a resistor is modeled as a parallel noise current source

$$I^2(f) = \frac{4kT}{R}$$

Flicker noise in CMOS transistors

The flicker noise spectral density at the gate of a CMOS transistor is

$$V^2(f) = \frac{K}{WLC_{ox}f}$$