## Lecture 4, ANIK

## Current mirrors

More on amplifiers (frequency domain)


## What did we do last time?

Voltage swing
How far can we push the transistors?
Target: Force all operate in saturation region

Ways to increase the gain?
0) Physical sizing

1) Electrical handles
2) Cascodes
3) Multiple stages

## What will we do today?

## Current mirrors

Simple, Wilson, Wide-Swing, Cascoded
Decoupling design parameters using current mirrors
Improved amplifier stages
Folded-cascoded gain stage
Gain-boosting
The frequency domain
Dominant-pole, DC gain, unity-gain frequency

Some kind of wrap-up session

## Current mirrors

Use currents to distribute references (low speed) over a chip

Receiver determines voltage across resistor

Resistance in wire does not matter

Local "ground" does not influence the result


## Current mirrors, cont'd

Use currents to bias amplifier stages Decouples the design parameters!

We can "ignore" the size and $v_{\text {eff }}$ of the bias transistor (active load)

Set the current through a reference of some kind


## Current mirrors, cont'd

Input (primary) should behave as a current sink, i.e., have

$$
Z_{i n}=0
$$

Output (secondary) should behave as a current source, i.e., have

$$
Z_{\text {out }}=0
$$



## Current mirrors



## Current mirrors, operation

The current relationship is given by the transistor sizes.
Notice that the $v_{e f f}$ is constant on the lower transistors.

$$
I_{\text {out }}=\frac{\alpha_{\text {out }}}{\alpha_{i n}} \cdot I_{i n}
$$

Compare with second-order model

$$
\frac{I_{\text {out }}}{I_{\text {in }}}=\frac{\alpha_{\text {out }}}{\alpha_{\text {in }}} \cdot \frac{1+\lambda v_{\text {out }}}{1+\lambda v_{\text {in }}}
$$

which will be too big of variations.

## Current mirrors, nonidealties

Voltage swing
Potential drops back and forth

Calculating the impedances Use the quick-trick from cascodes for cascodes


## Improved amplifier stages

Folded cascode
Common-source + common-gate

Same type of gain as in cascoded gain stage

Range increases (feedback configuration)

Why do we need the lower NMOS?


## Improved amplifier stages

Gain-boosting
Additional amplifier sets the gain of the cascode
"Output impedance is multiplied by cascode"

What about the swing now?


## Improved amplifier stages, cont'd

Folded cascode and gain boosting

Operation

Calculating the impedances Use the quick-tricks from cascodes for cascodes


## The frequency domain

Include the capacitor in your calculations


## The frequency domain

## Small-signal exercise <br> Impact of capacitor on common-source stage

Bode plot
Pole
DC gain
Unity-gain frequency


## Compilation

The overall transfer function

$$
A(s)=\frac{A_{0}}{1+\frac{s}{p_{1}}}=\frac{\frac{g_{m}}{g_{\text {out }}}}{1+\frac{s}{\frac{g_{\text {out }}}{C_{L}}}}
$$

Notice the trade-off between bandwidth and gain!

$$
A_{0} \cdot p_{1} \approx \omega_{u g}
$$

Very crucial in your OP amp design

## Amplifier stages, compiled 1

| Expression | CS | CD | CG*) |
| :---: | :---: | :---: | :---: |
| DC gain, $A_{0} \approx \frac{g_{m}}{g_{\text {out }}}$ | $\approx \frac{g_{m}}{g_{P}+g_{N}}$ | $\approx \frac{g_{m}}{g_{m}+g_{P}+g_{N}} \approx 1$ | $\approx \frac{g_{m}}{g_{P}+g_{N}}$ |
| Output impedance, $\approx g_{\text {out }}$ | $\approx g_{P}+g_{N}$ | $\approx g_{m}$ | $\approx g_{P}+g_{N}$ |
| Bandwidth, $p_{1} \approx \frac{g_{\text {out }}}{C_{L}}$ | $\approx \frac{g_{P}+g_{N}}{C_{L}}$ | $\approx \frac{g_{m}}{C_{L}}$ | $\approx \frac{g_{P}+g_{N}}{C_{L}}$ |
| Unity gain, $\approx A_{0} \cdot p_{1}$ | $\approx \frac{g_{m}}{C_{L}}$ | N/A (why?) | $\approx \frac{g_{m}}{C_{L}}$ |

## Amplifier stages, compiled 2

## Expression

DC gain, $A_{0} \approx \frac{g_{m}}{g_{\text {out }}}$

Output impedance, $\approx g_{\text {out }}$

Bandwidth, $p_{1} \approx \frac{g_{\text {out }}}{C_{L}}$
Unity gain, $\approx A_{0} \cdot p_{1}$

$$
\begin{array}{cr}
\mathbf{C S} & \mathbf{C D} \\
\approx \frac{1}{\lambda \cdot v_{e f f}} & \approx 1 \\
\hline
\end{array}
$$

$$
\approx \lambda I_{D}
$$

$$
\approx \frac{\lambda I_{D}}{C_{L}}
$$

$$
\approx \frac{I_{D}}{C_{L} \cdot v_{e f f}}
$$

$$
\approx \frac{2 I_{D}}{v_{e f f}}
$$

$$
\approx \frac{2 I_{D}}{C_{L} \cdot v_{e f f}}
$$

N/A (why?)

## CG*)

$$
\approx \frac{1}{\lambda \cdot v_{e f f}}
$$

$$
\approx \lambda I_{D}
$$

$$
\approx \frac{\lambda I_{D}}{C_{L} \cdot v_{e f f}}
$$

$$
\approx \frac{I_{D}}{C_{L} \cdot v_{e f f}}
$$

## Other tips-and-tricks

Common-drain
If the voltage levels are not good enough, you can shift up/down
Isolation of sensitive nodes (buffering)
"Current-stealing"
Consider the folded cascode amplifier. Notice that the two branches steal current from a common current source. Also remember that gain is inversely proportional to current. By stealing current, we can lower current, and thus increase gain.

## The transistor as a switch/resistor

The last operation

$$
I_{P N}=\alpha \cdot\left(2 V_{e f f} V_{d s}-V_{d s}^{2}\right)
$$

or

$$
I_{P N}=2 \alpha V_{d s} \cdot\left|V_{G}-V_{T}-\frac{V_{D}+V_{S}}{2}\right|
$$



Voltage dependent resistor, with conductance:

$$
\left.\left.G_{P N}=\frac{I_{P N}}{V_{d s}}=2 \alpha \cdot \right\rvert\, V_{G}-V_{T}-\frac{V_{D}+V_{S}}{2}\right)
$$

## The transistor as a switch/resistor

The linearized model

$$
G_{P N}=2 \alpha \cdot\left(V_{G}-V_{D}-V_{T}\right)
$$

What to think about

How to use it


## What did we do today?

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The switch

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## What will we do next time?

## Differential signals

Why differential?
Common-mode definitions
Differential pair
Analysis
Operation

Mismatch
Impact of mismatch on design/performance/behavior

