

Exercises for Tutorial 3: Frequency Response

- 1) Problem 6.6. in the course book.

a) $Z_{in} = \frac{g_{m1} + sC_1}{sg_{m1}C_1}$

b) $Z_{in} = \frac{sC_1C_2r_o + C_1 + C_2 + g_{m1}r_oC_2}{sC_1C_2(1 + g_{m1}r_o)} \quad (g_m = g_{m1} + g_{m2}, r_o = r_{o1} \parallel r_{o2})$

c) $Z_{in} = \frac{sC_2 + g_{m1}}{sC_2(g_{m1} + g_{mb1})}$

- 2) Problem 6.8(e) in the course book.

We define $C_1 = C_{gs1} + C_{sb1} + C_{db2} + C_{gd2}$, $C_2 = C_{gs2} + C_{sb2} + C_{db1} + C_{gd1}$

$$H(s) = \frac{V_{out}}{V_{in}} = \frac{g_{m1}}{s^2C_1C_2R_S + s((1 + g_{m1}R_S)C_2 + g_{m2}C_1R_S) + g_{m2}}$$

$$Z_{in} = \frac{g_{m2} + sC_2}{s^2C_1C_2 + s(g_{m1}C_2 + g_{m2}C_1)}$$

- 3) Problem 6.9(b) in the course book.

At low frequencies: $A_V \approx -g_{m1}r_{o3} \rightarrow \infty$ if $\lambda = 0$

At high frequencies: $A_V \approx -g_{m1}(r_{o1} \parallel r_{o3}) \rightarrow \infty$ if $\lambda = 0$

- 4) Problem 6.10(b) in the course book. Assume $r_{o3} \gg R_2$.

At low frequencies: $A_V \approx -g_{m1}R_2$

At high frequencies: $A_V \approx -\frac{g_{m1}g_{m6}R_1R_2}{2 + g_{m6}R_1}$

- 5) Figure 6 shows an amplifier schematic. For simplicity we can ignore all parasitics of M_1 and M_2 and we assume that the dominant pole occurs at the output node. Also, we assume $g_m \gg 1/r_o$. Find the product $|A_0|\omega_{-3dB}$, where A_0 is the DC gain and ω_{-3dB} is the 3 dB cut-off frequency. Assume $\gamma = 0$.

$$|A_0| \times \omega_{3dB} = \frac{g_{m2}}{C}$$

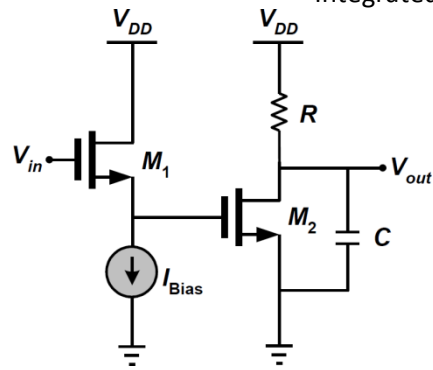


Figure 6 An amplifier schematic.

- 6) Figure 7 shows an amplifier schematic. For simplicity we can ignore all parasitics of $M_1 - M_4$ and we assume that the dominant pole occurs at the output node. If the input signal has an angular frequency of $\omega_i = 10^9 \text{ rad/s}$, determine the AC gain of the amplifier. Assume $g_{m1} = g_{m3} = 4 \text{ mA/V}$, $g_{m2} = g_{m4} = 1 \text{ mA/V}$, $C = 1 \text{ pF}$, $g_m \gg 1/r_o$ and $\gamma = 0$.

$$|A_{ac}| = 2\sqrt{2}$$

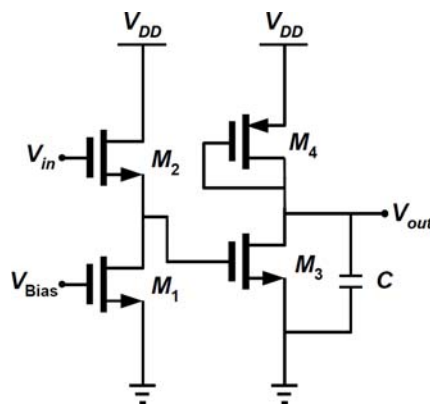


Figure 7 An amplifier schematic.