

## Solution to lecture 3 exercises

### 3-100

The diode 1 voltage will before turn-on ( $\omega t=0$ ) follow  $U_{ac}$  since D5 is conducting. During D1 conduction ( $0 < \omega t < 120\text{deg}$ ) the D1 voltage is ideally zero. After turn-off ( $\omega t=120\text{deg}$ ) the voltage is given by  $U_{ab}$  since D3 is turning on at this time. After D5 turn on ( $\omega t=240\text{deg}$ ) D1 voltage is given by  $U_{ac}$  until D1 again turns on at  $\omega t=360$ .

The diode 2 voltage will before turn-on ( $\omega t=60$ ) follow  $U_{bc}$  since D6 is conducting. During D2 conduction ( $60 < \omega t < 180\text{deg}$ ) the D2 voltage is ideally zero. After turn-off ( $\omega t=180\text{deg}$ ) the voltage is given by  $U_{ac}$  since D4 is turning on at this time. After D6 turn on ( $\omega t=300\text{deg}$ ) D2 voltage is given by  $U_{bc}$  until D2 again turns on at  $\omega t=60$ .

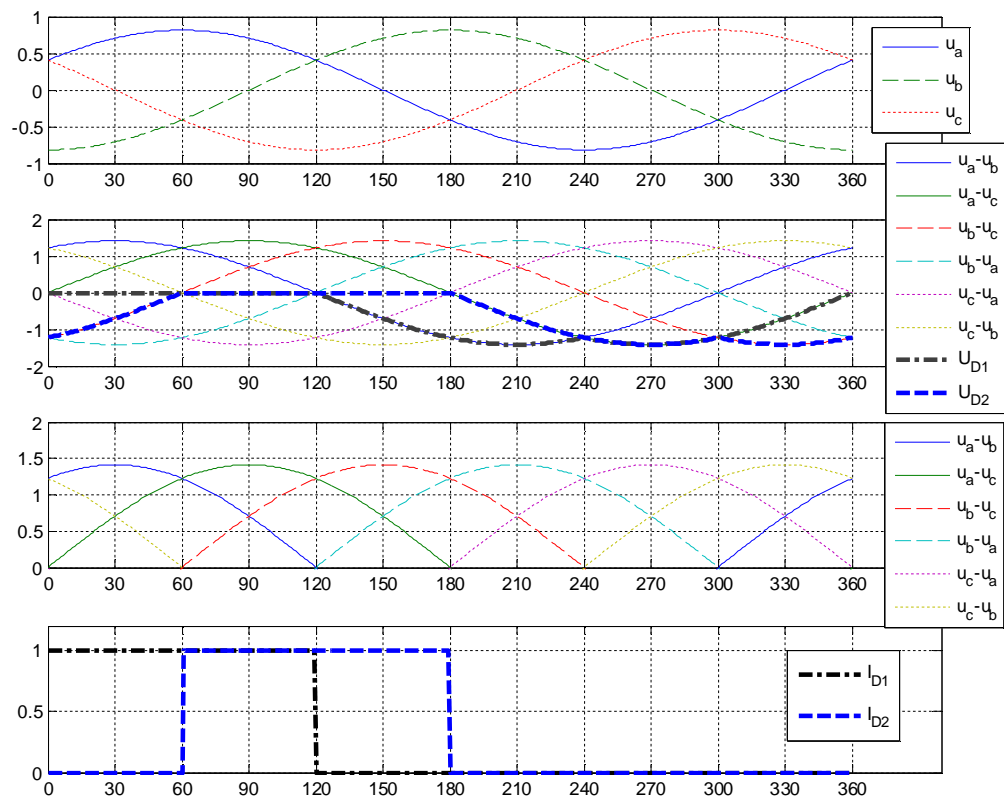


Figure 1

Tomas Jonsson

### 3-101

a)

$$I_s = \sqrt{2/3} \cdot I_d$$

$$I_{s\max} = 10 \text{ Arms}$$

$$\Rightarrow I_{d\max} = 12.2 \text{ A}$$

b)

$$U_{d0} = 1.35 \cdot 400 = 540 \text{ V}$$

$$\Delta U_d = \frac{3}{\pi} \omega L_s I_d = 25.6 \text{ V}$$

$$U_d = U_{d0} - \Delta U_d = 514 \text{ V}$$

c)

$$P_{\max} = U_d \cdot I_{d\max} = 6.3 \text{ kW}$$

d)

See Figure 1 above.

$$\text{Average diode D1 current is } I_{D1AV} = \frac{1}{2\pi} \int_0^{2\pi/3} I_{D1} d\omega t = \frac{I_d}{3} = 4.1 \text{ A}$$

e)

See Figure 1 above.

$$\text{RMS diode current is: } I_{D1RMS} = \sqrt{\frac{1}{2\pi} \int_0^{2\pi/3} I_{D1}^2 d\omega t} = \sqrt{\frac{1}{3}} I_d = 7.1 \text{ A}$$

### 3-102

Diode conduction losses:

$$P_{av} = \frac{1}{2\pi} \int_0^{2\pi/3} (V_0 i_{D1} + R_s i_{D1}^2) d\omega t = V_0 i_{D1AV} + R_s i_{D1RMS}^2 =$$

$$= 0.79 \cdot 4.1 + 0.013 \cdot 7.1^2 = 3.9 \text{ W}$$

Total rectifier losses are  $6 \cdot 3.9 = 24 \text{ W}$

Losses in % of the load =  $24/6300 = 0.4\%$