

Exercises for Tutorial 6: Timing issues

1. Assume that an inverter stage can be approximated as a first-order circuit with a single pole at ω_0 and a stage gain of $-A$. Determine the open-loop transfer function of a 5-stage ring oscillator. Calculate the minimum required voltage gain per stage in order to have oscillation.
2. A voltage-controlled oscillator with linear tuning characteristic has a gain of $2\pi \times 10^8 \frac{\text{rad}}{\text{s}}/\text{V}$. The control voltage varies between 0 and 3 V. When the control voltage is 0.5 V, the oscillation frequency is 1 GHz. Calculate the required control voltage to get 1.25 GHz oscillation frequency.
3. Consider the PLL loop filter circuit shown in Figure 13. Determine the transfer function $G(s)$ of this filter. The op-amp is ideal.

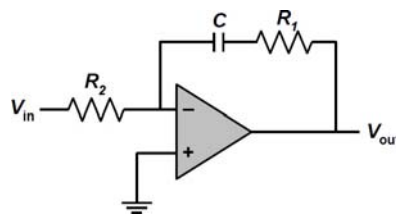


Figure 13 Loop filter circuit.

4. A block diagram of a PLL is shown in Figure 14. ϕ_{in} is the reference phase and ϕ_{out} is the output of the oscillator. The following relations can be identified:

$$V_1 = K_{PD}(\phi_{in} - \phi_{out})$$

$$\frac{d\phi_{out}}{dt} = K_{VCO}V_2$$

- a) Determine the closed-loop transfer function of the PLL from ϕ_{in} to ϕ_{out} . Use the loop filter transfer function $G(s)$ in problem 3.
- b) What are the necessary conditions on K_{PD} and K_{VCO} for stability?

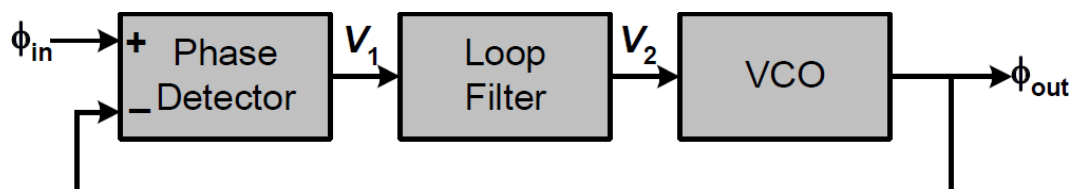


Figure 14 PLL block diagram.