## EXAMINATION IN

## TSEK03

## Radio Frequency Integrated CIRCUITS

```
Date:
    2015-03-19
Time:
    8-12
Location:
    TER2
Tools:
    Calculator, Dictionary
Teachers:
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12 points are required to pass.
(12-16: 3, 16-20: 4, 20-24: 5)

Please start each new problem at the top of a page! Only use one side of each paper!

## 1.

Consider the common-gate broadband amplifier below.
a. Derive an expression for the noise figure in the absence of gate noise. Select the transistor's $g_{m}$ for use as an LNA. Neglect transistor capacitances, body effect, and channel-length modulation. (3 p)
b. Re-derive the noise figure, now taking gate noise into account. Hint: Model the gate noise using a voltage source of $4 \mathrm{kTR}_{\mathrm{G}} / 3$. (1 p)

${ }^{\wedge} 2$.
Consider the resistively shunted common-source amplifier shown in the figure below.
a. Derive expressions for gain, input impedance and noise figure for the amplifier. Neglect gate noise and noise from the load resistor as well as transistor capacitances, body effect, and channel-length modulation. (3p)
b. When used in a $50 \Omega$ system ( $R_{S}=50 \Omega$ ), how should $R_{\text {sh }}$ be selected so that the amplifier is best suited as an Rx-LNA? Simplify the NF expression using this value! (1 p)


## 3.

Shown in the figure below is the frontend of a $1.8-\mathrm{GHz}$ receiver. The LO frequency is chosen to be 900 MHz and the load inductors and capacitances resonate with a quality factor of $Q$ at IF. Assume $M_{1}$ is biased at a current of $I_{1}$, the mixer and the LO are perfectly symmetric, and $M_{2}$ and $M_{3}$ switch abruptly and completely.

Compute the LO-IF feedthrough, i.e., the measured level of the $900-\mathrm{MHz}$ output component in the absence of an RF signal. Model the inductor losses with parallel resistors, $Q=R_{p} /\left(\omega_{0} L_{p}\right)$. (3p)

4.

A negative resistance LC oscillator used for carrier generation in a 3G uplink transmitter is shown here.

The component values are $\mathrm{L}=2 \mathrm{nH}$ and $\mathrm{C}=3 \mathrm{pF}$.
$Q$ of the inductors around the relevant frequency is 5 .
$L_{p}=\left(1+1 / Q^{2}\right){ }^{*} L_{s}, R_{p}=\left(Q^{2}+1\right)^{*} R_{s}$
$\mathrm{I}_{\mathrm{B}}=1 \mathrm{~mA}, \mu_{\mathrm{n}^{*}} \mathrm{C}_{0 \mathrm{x}}=200 \mu \mathrm{~A} / \mathrm{V}^{2}$.
a. Calculate the oscillation frequency, neglecting losses in the inductors. ( 1 p )
b. Calculate the oscillation frequency, including losses in the inductors. How much does the oscillation frequency change, and in what direction, when inductor losses are included? (1 p)
c. What is the required width in $\mu \mathrm{m}$ of M 1 and M 2 to ensure oscillation? We will use the minimum transistors in a 65 nm CMOS technology (Ldrawn $=0.060$ um) which are operated at $\mathrm{V}_{\mathrm{DD}}=1.2 \mathrm{~V}$. Assume that the electrical channel length is the same as Ldrawn and neglect all parasitics associated with the transistors. (2 p )


## 5.

For the frequency-multiplying PLL shown below, determine the:
a. closed-loop transfer function
(2 p)
b. damping factor $\zeta$
c. natural frequency $\omega_{n}$
d. loop bandwidth
(1 p)

6.
a. The following table lists three different properties for the $A, B, C, D$, and $E$ power amplifier classes and their typical values. Identify the power amplifier class for each column. ( 2.5 p )

| Maximum drain efficiency <br> [\%] | 100 | 78.5 | 100 | 50 | 100 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Peak drain voltage [*V ${ }^{*}$ D] |  |  |  |  |  |

b. How would you select the gate-bias $\mathrm{V}_{\mathrm{g}, \mathrm{bias}}$ for a class-AB power amplifier? (0.5 p)
c. What are the performance trade-offs when choosing this $\mathrm{V}_{\mathrm{g}, \mathrm{bias}}$-value? ( 0.5 p )
d. What is the purpose of a "load-pull characterization" of a power amplifier? (0.5 p)

## TRANSISTOR EQUATIONS

NMOS


PMOS


## NMOS

- Cutoff:

$$
\mathrm{I}_{\mathrm{D}}=0 \quad\left(\mathrm{~V}_{\mathrm{GS}}<\mathrm{V}_{\mathrm{TN}}\right)
$$

- Linear mode:

$$
I_{D}=\mu_{n} C_{o x} \frac{W}{L}\left(\left(V_{G S}-V_{T N}\right) V_{D S}-\frac{V_{D S}^{2}}{2}\right) \quad\left(\mathrm{V}_{\mathrm{GS}}>\mathrm{V}_{\mathrm{TN}}\right) \text { and }\left(\mathrm{V}_{\mathrm{DS}}<\mathrm{V}_{\mathrm{GS}}-\mathrm{V}_{\mathrm{TN}}\right)
$$

- Saturation mode:

$$
I_{D}=\frac{1}{2} \mu_{n} C_{o x} \frac{W}{L}\left(V_{G S}-V_{T N}\right)^{2}\left(1+\lambda V_{D S}\right) \quad\left(\mathrm{V}_{\mathrm{GS}}>\mathrm{V}_{\mathrm{TN}}\right) \text { and }\left(\mathrm{V}_{\mathrm{DS}}>\mathrm{V}_{\mathrm{GS}}-\mathrm{V}_{\mathrm{TN}}\right)
$$

## PMOS

- Cutoff:

$$
\mathrm{I}_{\mathrm{D}}=0 \quad\left(\mathrm{~V}_{\mathrm{GS}}<\left|\mathrm{V}_{\mathrm{TP}}\right|\right)
$$

- Linear mode:

$$
I_{D}=\mu_{p} C_{o x} \frac{W}{L}\left(\left(V_{S G}-\left|V_{T P}\right|\right) V_{S D}-\frac{V_{S D}^{2}}{2}\right) \quad\left(\mathrm{V}_{\mathrm{GS}}>\left|\mathrm{V}_{\mathrm{TP}}\right|\right) \text { and }\left(\mathrm{V}_{\mathrm{SD}}<\mathrm{V}_{\mathrm{SG}}-\left|\mathrm{V}_{\mathrm{TP}}\right|\right)
$$

- Saturation mode:

$$
I_{D}=\frac{1}{2} \mu_{p} C_{o x} \frac{W}{L}\left(V_{S G}-\left|V_{T P}\right|\right)^{2}\left(1+\lambda V_{S D}\right) \quad\left(\mathrm{V}_{\mathrm{GS}}>\left|\mathrm{V}_{\mathrm{TP}}\right|\right) \text { and }\left(\mathrm{V}_{\mathrm{SD}}>\mathrm{V}_{\mathrm{SG}}-\left|\mathrm{V}_{\mathrm{TP}}\right|\right)
$$

