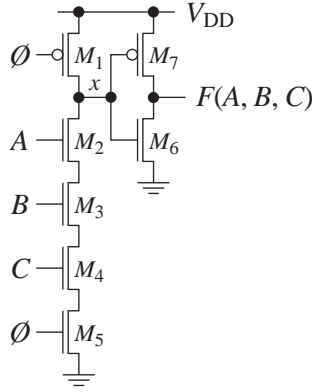


TSTE03 Homework 3: Solution

Inspect layout \Rightarrow

Schematic



Function

$$S_n = ABC \Rightarrow x = (ABC)' \Rightarrow \boxed{F = ABC}$$

Gate, source, and drain widths

$$W_1 = W_2 = W_3 = W_4 = W_5 = W_6 = 0.5 \mu\text{m}, W_7 = 1.0 \mu\text{m}$$

Gate lengths

$$L_1 = L_2 = L_3 = L_4 = L_5 = L_6 = L_7 = 0.25 \mu\text{m}$$

Source lengths

$$L_{s1} = L_{s5} = L_{s6} = L_{s7} = 0.5 \mu\text{m}, L_{s2} = L_{s3} = L_{s4} = 0.25 \mu\text{m}$$

Drain lengths

$$L_{d1} = L_{d2} = L_{d6} = L_{d7} = 0.75 \mu\text{m}, L_{d3} = L_{d4} = L_{d5} = 0.25 \mu\text{m}$$

Metal wire dimensions of node x

$$W_m = 0.375 \mu\text{m}, L_m \approx 7 \mu\text{m}$$

Poly wire dimensions of node x

$$W_p = 0.25 \mu\text{m}, L_p \approx 4 \mu\text{m}$$

Worst-case PMOS drain capacitance of node x

$$\begin{aligned} C_{d1} &\approx W_1 L_{d1} C_{j0p} + (W_1 + 2L_{d1}) C_{jsw0p} = \\ &= 0.5 \cdot 10^{-6} \cdot 0.75 \cdot 10^{-6} \cdot 1.9 \cdot 10^{-3} + (0.5 \cdot 10^{-6} + 2 \cdot 0.75 \cdot 10^{-6}) \cdot 0.22 \cdot 10^{-9} \text{ F} \approx 1.16 \text{ fF} \end{aligned}$$

Worst-case NMOS drain capacitance of node x

$$\begin{aligned} C_{d2} &\approx W_2 L_{d2} C_{j0n} + (W_2 + 2L_{d2}) C_{jsw0n} = \\ &= 0.5 \cdot 10^{-6} \cdot 0.75 \cdot 10^{-6} \cdot 2.0 \cdot 10^{-3} + (0.5 \cdot 10^{-6} + 2 \cdot 0.75 \cdot 10^{-6}) \cdot 0.28 \cdot 10^{-9} \text{ F} \approx 1.31 \text{ fF} \end{aligned}$$

Worst-case gate capacitance of MOSFETs $M_1 \dots M_6$

$$C_{g1} = C_{g2} = C_{g3} = C_{g4} = C_{g5} = C_{g6} \approx W_i L_i C_{ox} = 0.5 \cdot 10^{-6} \cdot 0.25 \cdot 10^{-6} \cdot 6 \cdot 10^{-3} \text{ F} = 0.75 \text{ fF}$$

Worst-case gate capacitance of MOSFET M_7

$$C_{g7} \approx W_7 L_7 C_{ox} = 1.0 \cdot 10^{-6} \cdot 0.25 \cdot 10^{-6} \cdot 6 \cdot 10^{-3} \text{ F} = 1.5 \text{ fF}$$

Capacitance of metal wire of node x

$$\begin{aligned} C_m &\approx W_m L_m C_{ma} + 2(W_m + L_m) C_{mf} = \\ &= 0.375 \cdot 10^{-6} \cdot 7 \cdot 10^{-6} \cdot 35 \cdot 10^{-6} + 2(0.375 \cdot 10^{-6} + 7 \cdot 10^{-6}) \cdot 55 \cdot 10^{-12} \text{ F} \approx 0.91 \text{ fF} \end{aligned}$$

Capacitance of poly wire of node x

$$\begin{aligned} C_p &\approx W_p L_p C_{pa} + 2(W_p + L_p) C_{pf} = \\ &= 0.25 \cdot 10^{-6} \cdot 4 \cdot 10^{-6} \cdot 75 \cdot 10^{-6} + 2(0.25 \cdot 10^{-6} + 4 \cdot 10^{-6}) \cdot 40 \cdot 10^{-12} \text{ F} \approx 0.42 \text{ fF} \end{aligned}$$

Worst-case capacitance of node x

$$C_x \approx C_{d1} + C_{d2} + C_{g1} + C_{g2} + C_{g6} + C_{g7} + C_m + C_p \approx \boxed{7.6 \text{ fF}}$$

Initial state for worst case charge sharing is when all internal capacitances are discharged

- $A = 0$ turns off path to rest of the switch net
- $B = C = \emptyset = 1$ discharges the capacitances in the switch net

Output node x should then be precharged with no charging of internal capacitances

- $A = 0$ turns off path to rest of the switch net
- $\emptyset = 0$ precharges node x
- State of B and C does not matter since associated capacitances are already discharged

Worst case charge sharing occurs when the output node x shares its charge with internal ones

- $\emptyset = 1$ makes node x dynamic
- $A = B = 1$ connects node x to the switch net nodes and shares the charge
- $C = 0$ is needed for evaluating x to 1

Answers

- Implemented function is $F = ABC$
- Worst-case parasitic capacitance at node x is $C_x \approx 7.6$ fF
- Largest charge sharing occurs for $\langle \emptyset, A, B, C \rangle = \langle 1, 0, 1, 1 \rangle \rightarrow \langle 0, 0, -, - \rangle \rightarrow \langle 1, 1, 1, 0 \rangle$